

# Chapter 4 Computational design of metal systems

- An overview on metals
- 0-Dimensional System: magic clusters
- **Growth of quantum-sized metallic films**
  - One Dimensional Metal System: Metal Atom Wires
  - Two Dimensional Metal System:
    - A brief overview of quantum growth
    - From precise structural control to property optimization
- Nano Plasmonics

# This Topics is Contributed by (Partial List)

Prof. Chih-Kang Shih	@	Univ. of Texas at Austin
Prof. Qian Niu	@	Univ. of Texas at Austin
Prof. Hanno Weitering	@	Univ. of Tennessee/ORNL
Prof. James Thompson	@	Univ. of Tennessee/ORNL
Prof. Jun-Hyung Cho	@	Hanyang Univ./ORNL
Prof. Yu Jia	@	Zhengzhou Univ./ORNL
Prof. Biao Wu	@	Institute of Physics, CAS
Dr. Murat Ozer	@	Univ. of Tennessee/ORNL
Dr. Wenguang Zhu	@	Univ. of Tennessee/ORNL
Dr. Alex Khajetoorians	@	Univ. of Texas at Austin
Dr. Enju Yoon	@	Univ. of Tennessee
Guangfen Wu	@	Southeastern Univ./UT
Dr. Haiping Lan	@	USTC
Dr. Ping Cui	@	USTC

.

One Dimensional Metal System:  
**Metal Atom Wires**

# Quantum Size Effect and Electronic Stability of Free-standing Metal Atom Wires

Haiping Lan<sup>1</sup>

Ping Cui<sup>1</sup>

Jun-Hyung Cho<sup>3</sup>

Qian Niu<sup>4</sup>

Jinlong Yang<sup>1</sup>

Zhenyu Zhang<sup>1,2</sup>

<sup>1</sup>University of Science and Technology of China

<sup>2</sup>University of Tennessee at Knoxville

<sup>3</sup>Hanyang University, Korea

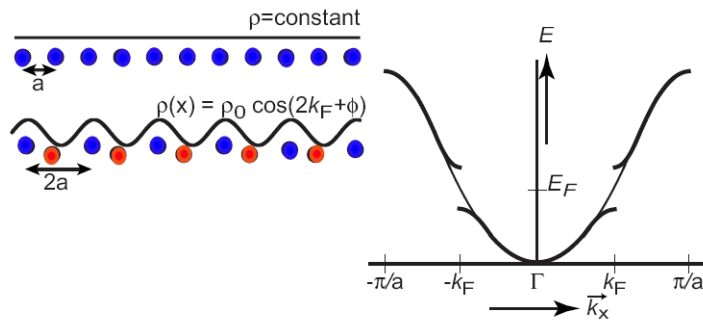
<sup>4</sup>University of Texas at Austin

Supported by NSF of China and USDOE

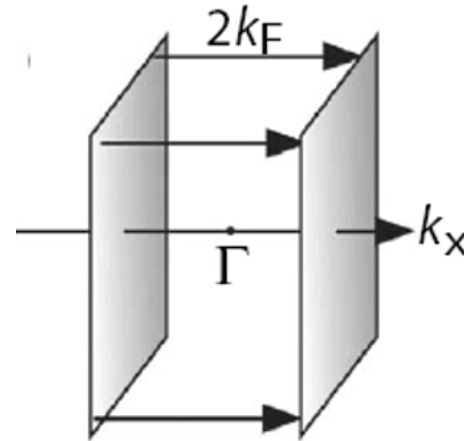


# Exotic Properties of 1-D Systems

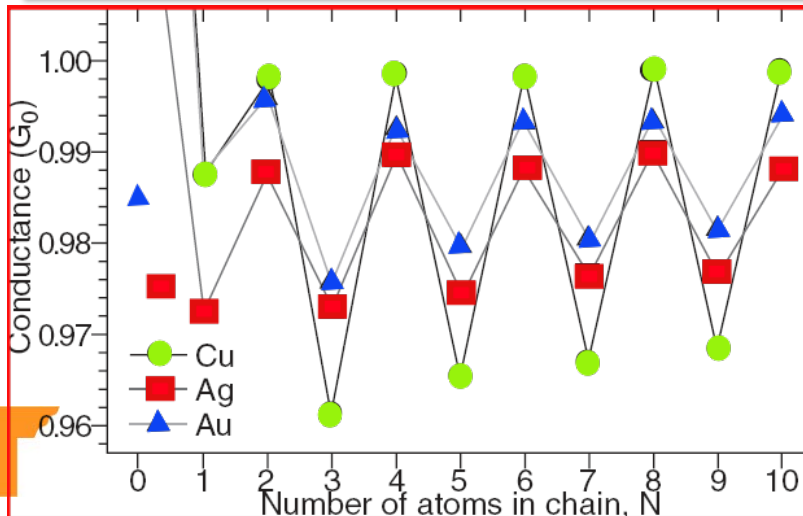
## Peierls instability



## Perfectly nested Fermi surface



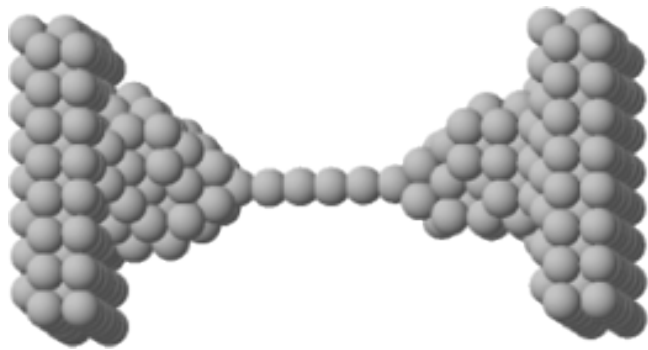
## Conductance quantization



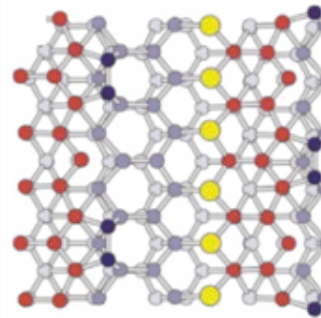
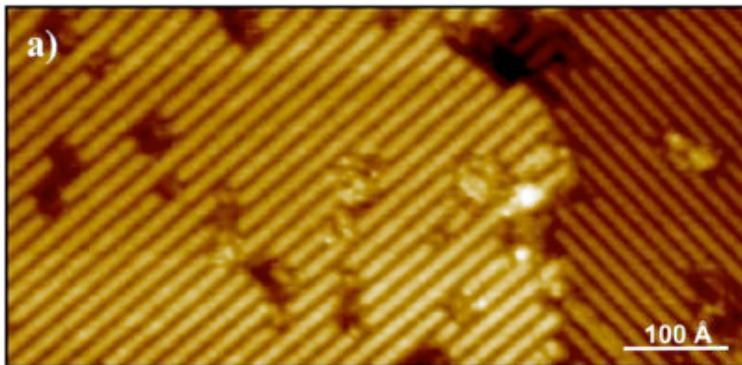
## Non-Fermi liquid, Charge-spin decoupling

# Fabrications of Metal Atom Wires

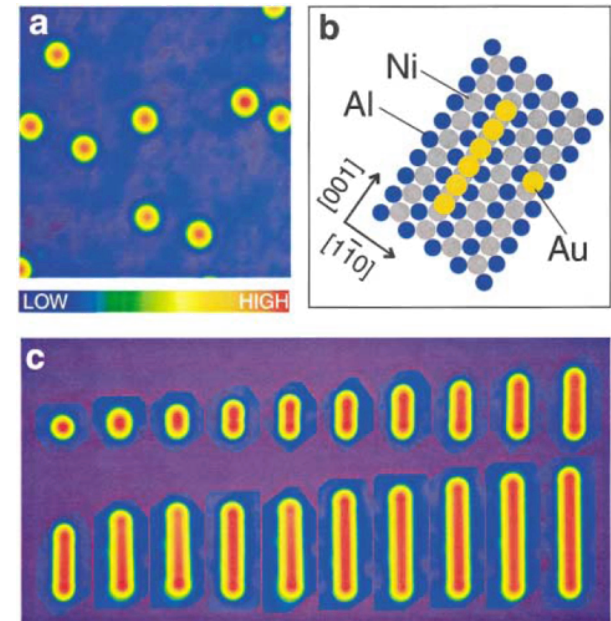
## Mechanical break junctions



## Self-assembly on substrates



## Manipulation by SPM

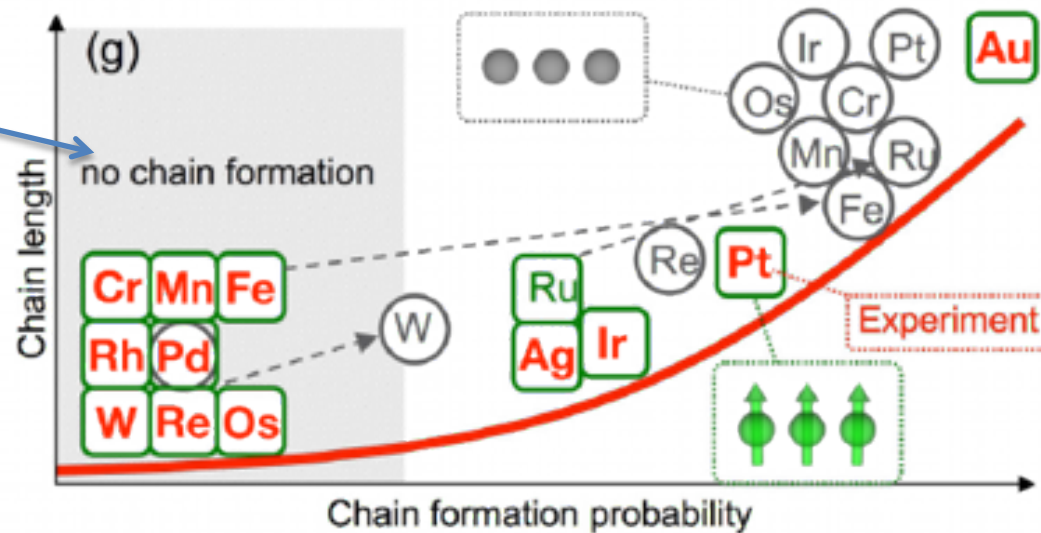


- Snijders, *et al*, RMP, **82**, 307(2010),
- Nilus, *et al*, Science, **297**,1853 (2002)

# Formation Mechanisms of Metal Atom Wires

## Mechanical break junctions

The creation of magnetic moments crucially reduces the probability of successful chain formation, and causes softening of the binding energy of atomic chains.



*sd* competition caused by the relativistic effects

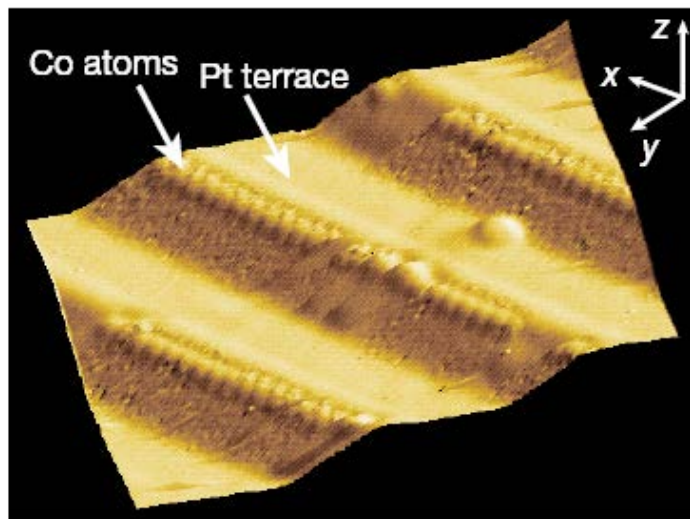
⇒ 5d metals prefer to form chains

- Bahn, *et al*, Phys. Rev. Lett, **87**, 266101 (2001)
- Smit, *et al*, Phys. Rev. Lett, **87**, 266102 (2001)
- Thiess, *et al*, Phys. Rev. Lett, **103**, 217201(2009)

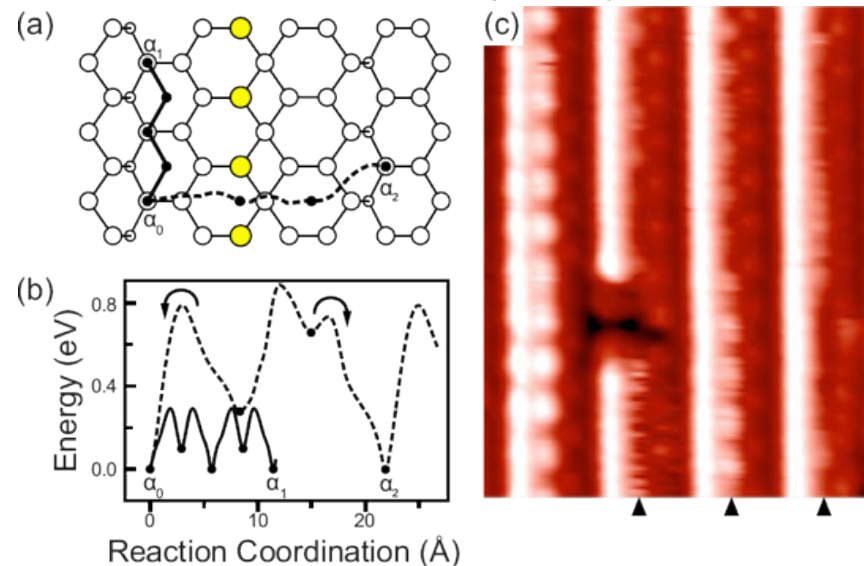
# Formation Mechanisms of Metal Atom Wires

## Self-Assembly

Co on Pt(111)

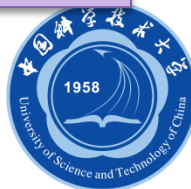


In on Si(553)-Au



**Anisotropic surfaces as growth templates:** The microscopic mechanism of the templated self-assembly is due to well-aligned preferential adsorption sites and the strongly anisotropic surface diffusion.

- Oncel, *et al*, J. Phys.: Condens.Matter, **20**, 393001 (2008)
- Kang, *et al*, Phys. Rev. B, **79**, 113403 (2009)
- Gambardella, *et al*, Nature, **416**, 301 (2002)

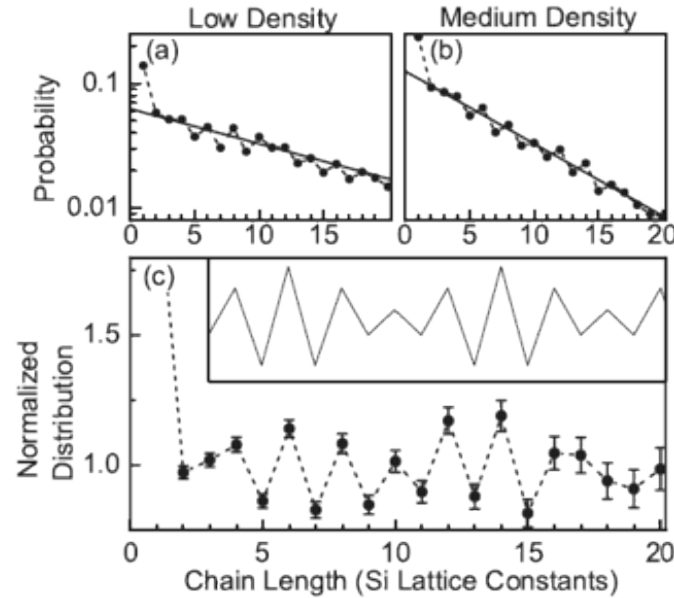
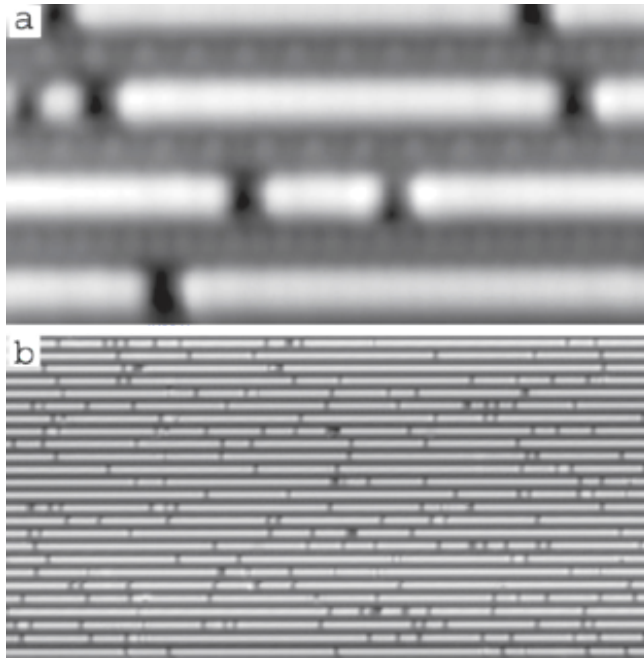




# Size Distribution of Atom Wires

Au on Si(553)

- Crain, *et al*, Phys. Rev. Lett, **96**,156801(2006)



Gold deposited on Si(553) leads to self-assembly of atomic chains, which are broken into finite segments by defects.

STM study provides the distribution of chain lengths and the correlation between defects that separate the chains. The length distribution reveals oscillations, indicating changes in the cohesive energy as a function of chain length.

Even-odd oscillation up to 16 atoms

# Representative Systems & Calculation Settings

s		sd		sp		sp <sup>2</sup>	
lithium 3 <b>Li</b> 6.941							
sodium 11 <b>Na</b> 22.990			aluminium 13 <b>Al</b> 26.982			silicon 14 <b>Si</b> 28.086	
potassium 19 <b>K</b> 39.098	copper 29 <b>Cu</b> 63.546		gallium 31 <b>Ga</b> 69.723			germanium 32 <b>Ge</b> 72.61	
rubidium 37 <b>Rb</b> 85.468	silver 47 <b>Ag</b> 107.87		indium 49 <b>In</b> 114.82			tin 50 <b>Sn</b> 118.71	
caesium 55 <b>Cs</b> 132.91	gold 79 <b>Au</b> 196.97		thallium 81 <b>Tl</b> 204.38			lead 82 <b>Pb</b> 207.2	

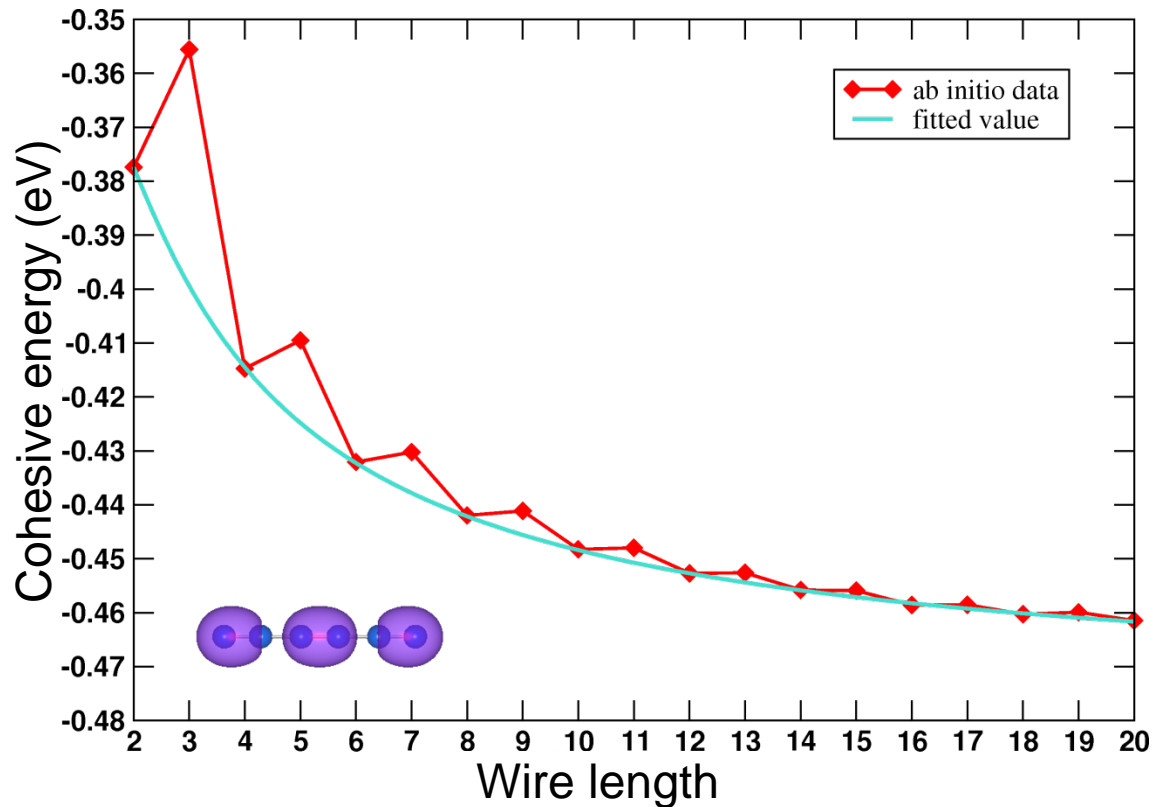
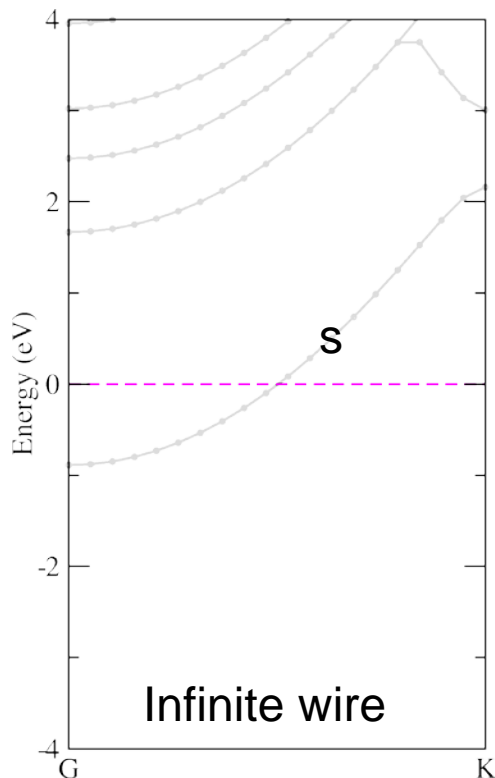
- Up to 20 atoms



- DFT
- PAW
- PBE
- Images separation > 10.0 Å
- CG scheme for relaxation
- Residual force < 0.01 eV/Å
- Cohesive energy:

$$E_c(n) = (E_{\text{wire}}(n) - n \cdot E_{\text{atom}}) / n$$

# s electron system - Na ( $3s^1$ ) atom wires



Electrons pairing up



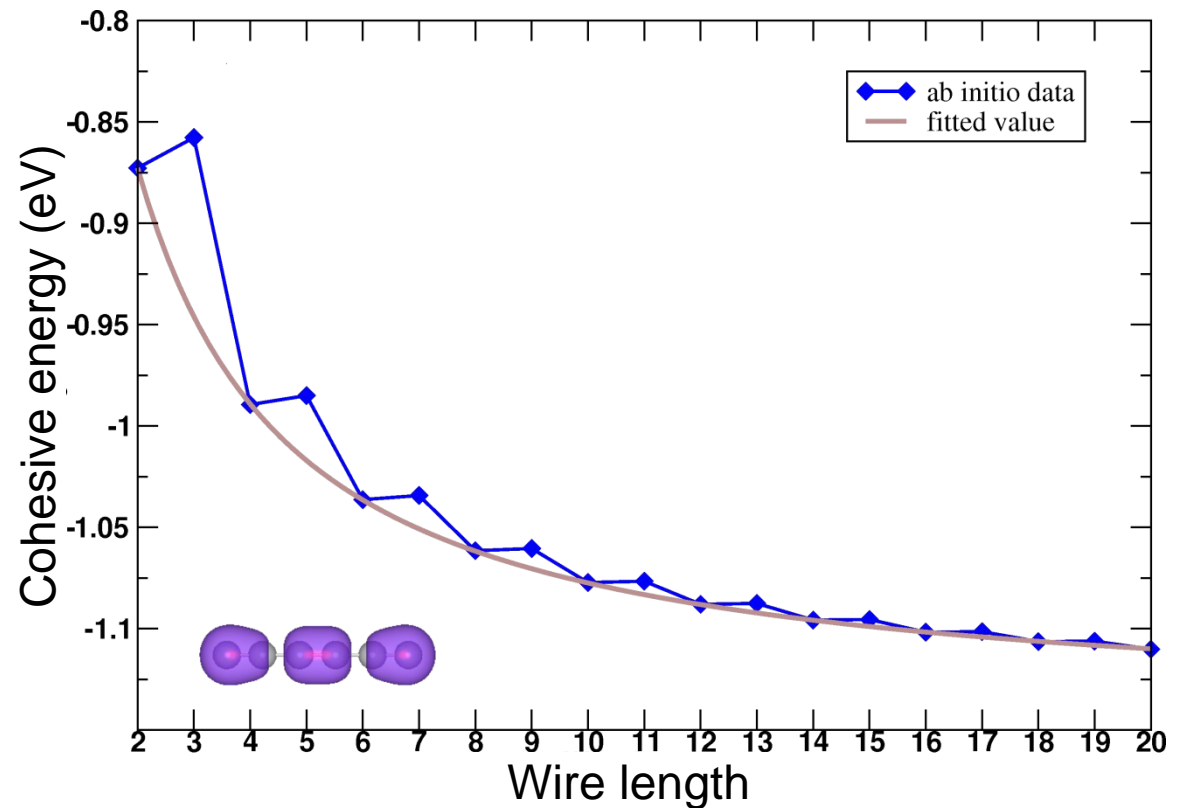
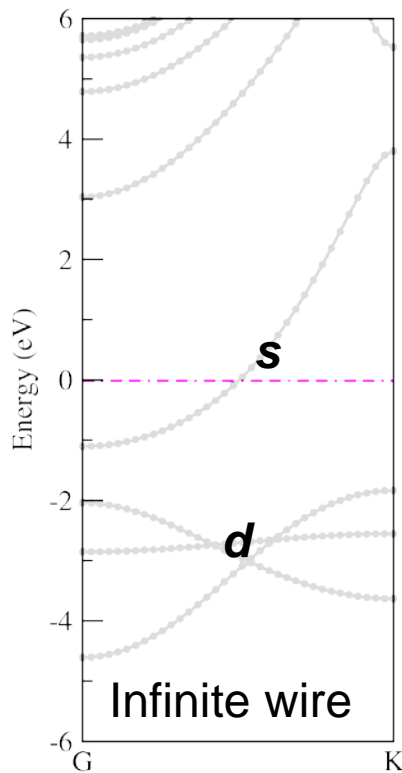
Even-odd oscillation

1-D confinement



$1/r$  nature

# *sd* electron system – Ag ( $4d^{10}.5s^1$ ) atom wires



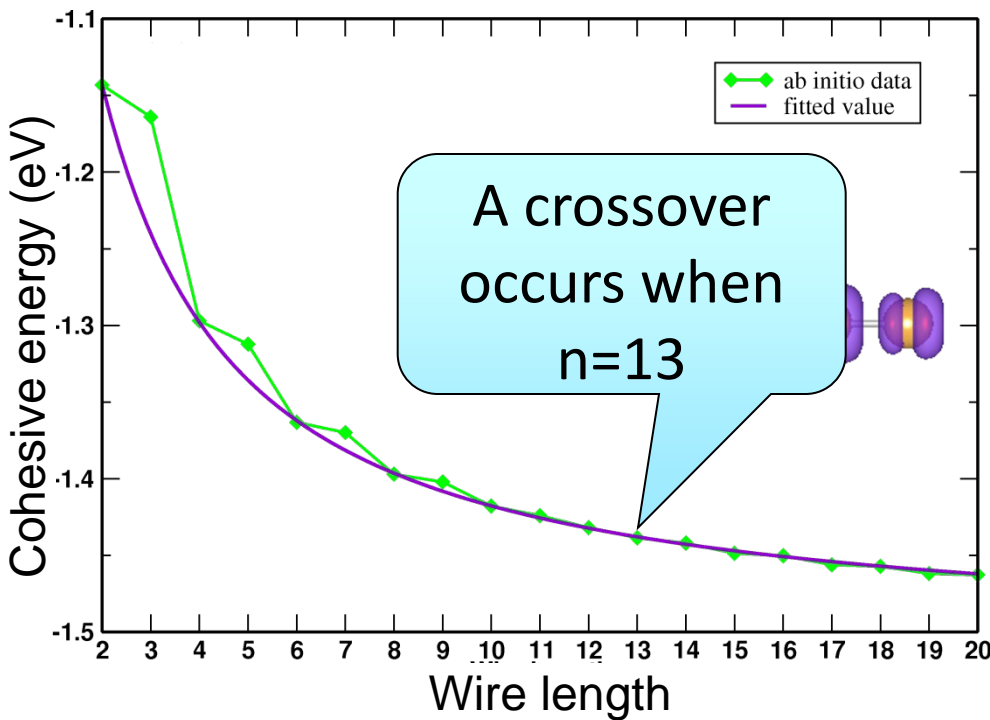
The same behavior as Na wires

*sd* hybridization

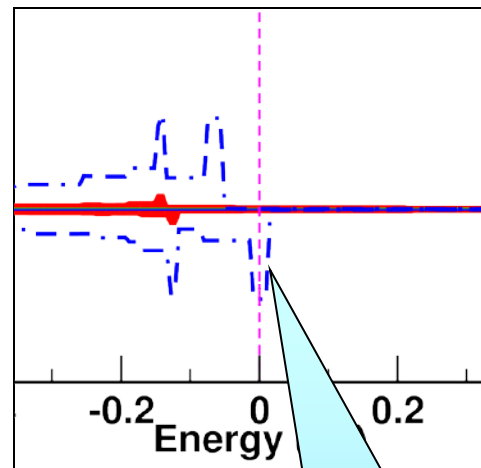


Larger cohesive energy

# *sd* electron system - Au ( $5d^{10}.6s^1$ ) atom wires



Infinite wire



Stoner instability  
Magnetic moment

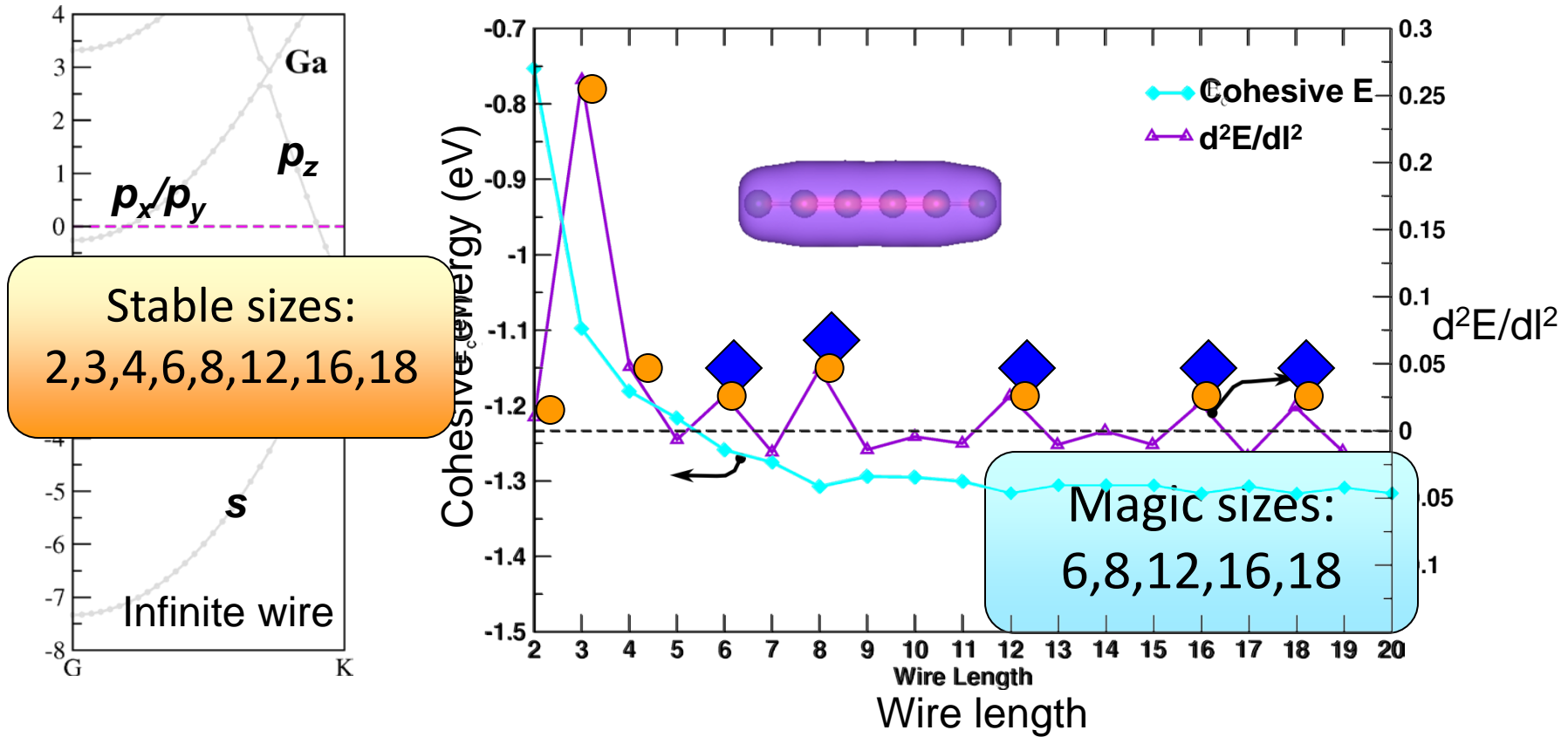
Relativistic effect



A bit large oscillation



# *sp* electron system - Ga ( $4s^2.4p^1$ ) atom wires

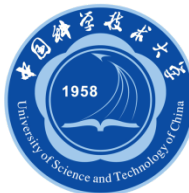


Little *sp* hybridization

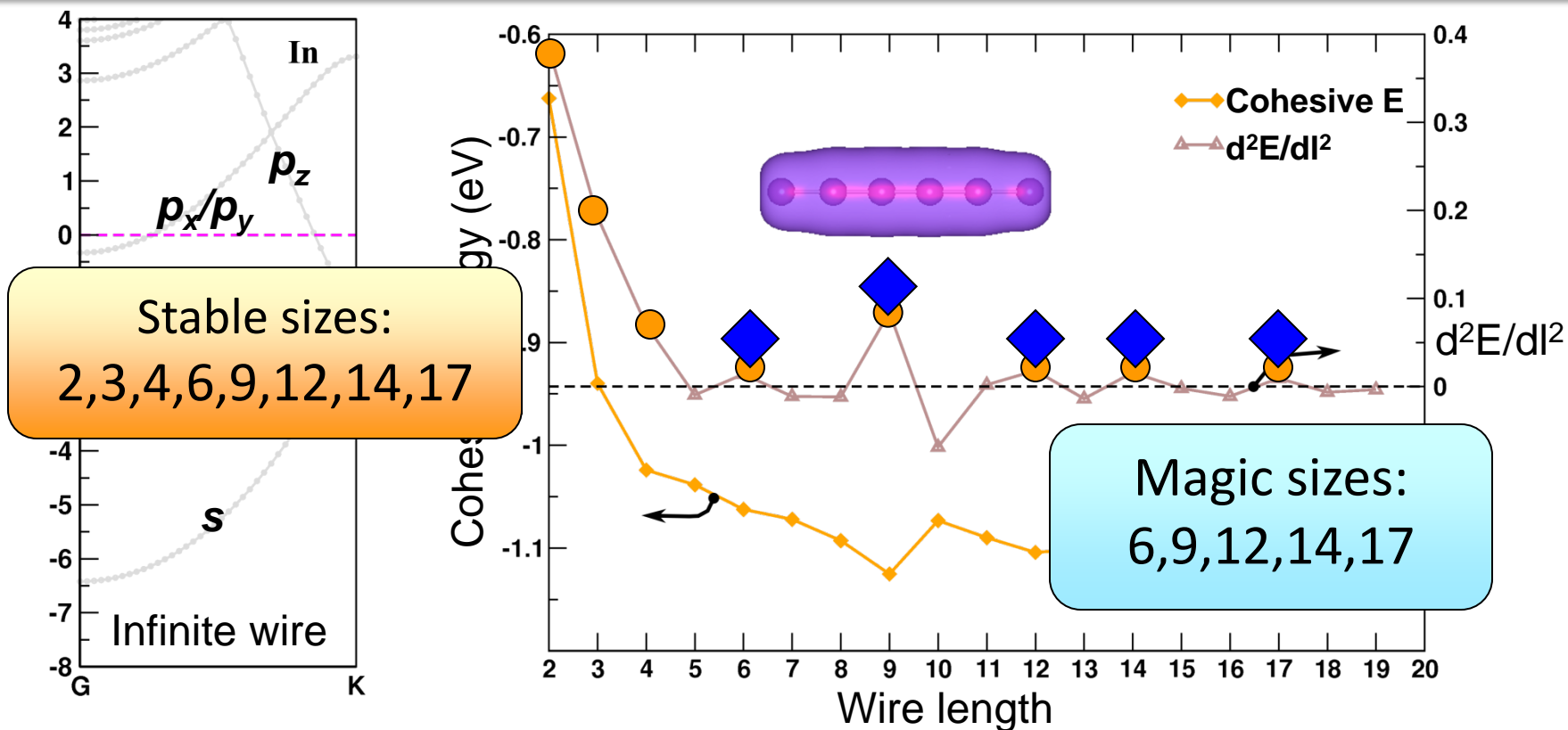


Only *p* electron contributes binding

An oscillation beyond the even-odd pattern



# *sp* electron system - In ( $5s^2.5p^1$ ) atom wires



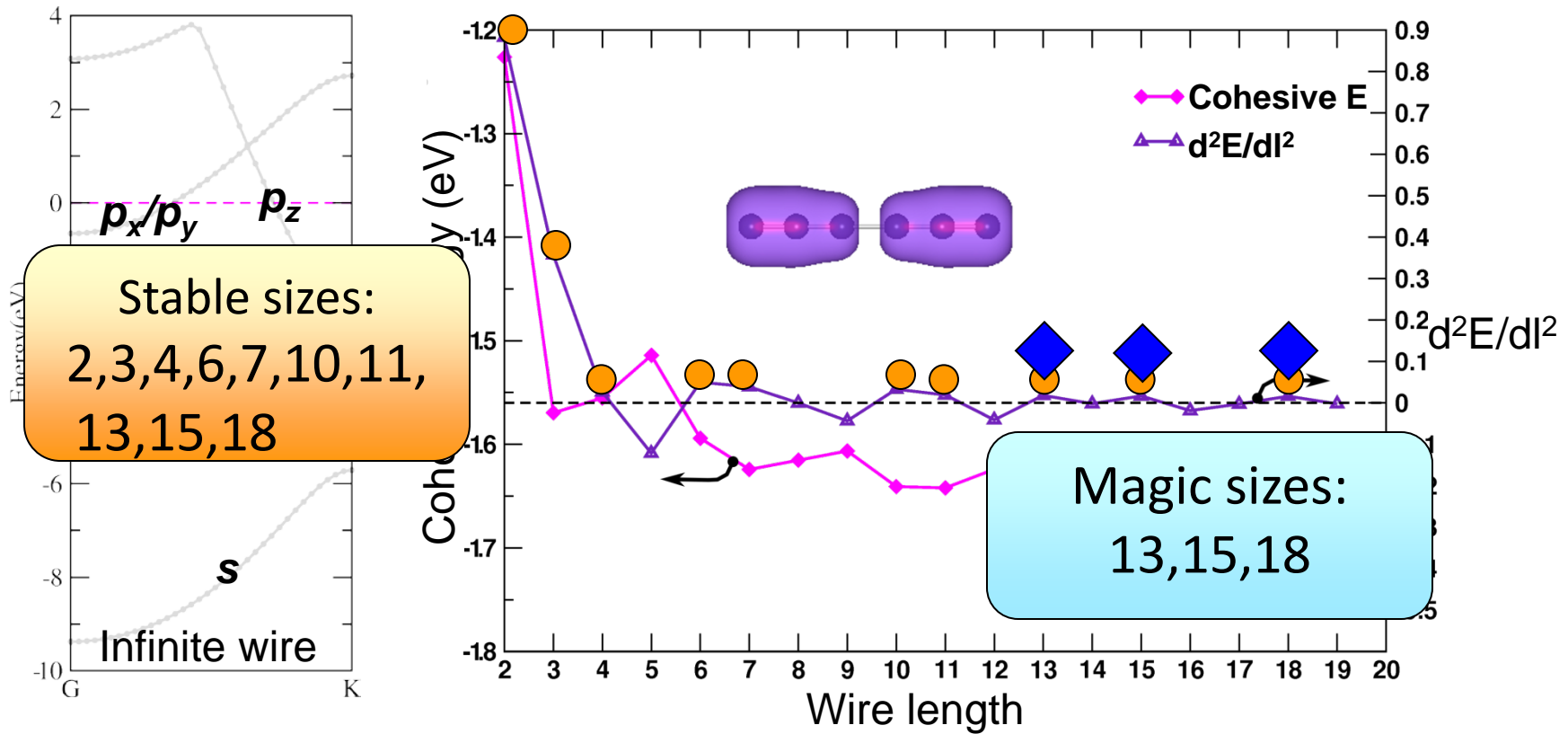
A similar behavior as Ga wires

Distinction between Ga and In

Nuclei radius



# $sp^2$ electron system - Pb ( $6s^2.6p^2$ ) atom wires



Little  $sp$  hybridization



Only  $p$  electrons contribute to binding



# Conclusions

## Electronic nature of freestanding atom wires' stability

Cohesive energy versus wire length indicates the existence of preferred (or magic) lengths, but with different characteristics.

➤ ***s*-electron system – Na, K: even-odd oscillation**

consecutive fillings of the *s* electrons in the quantum well states

➤ ***sd*-electron system – Ag, Au: even-odd oscillation**

*s* states dominate due to the filled shells of the *d* states

➤ ***sp*-electron system – Ga, In: complex oscillation**

minimal contributions of the filled *s* states and the dominance of the partially-filled *p* orbitals



## **Two Dimensional Metal System:**

- A brief overview of quantum growth
- From precise structural control to property optimization

*A Brief Review on*

# **Quantum Stability of 2D Metal Overlayers**

Zhenyu Zhang, Qian Niu, Chih-Kang Shih, PRL (1998)

Zhigang Suo and Zhenyu Zhang, PRB (1998)

·  
·  
·

# Classical Growth Modes in Heteroepitaxy (A/B)

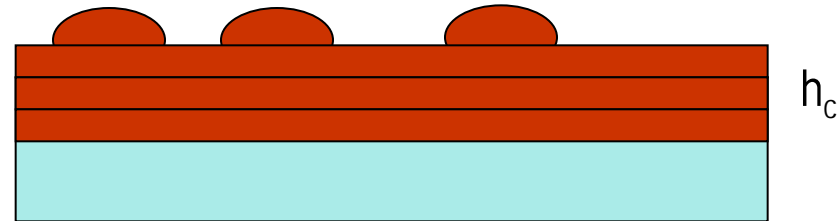
(Bauer, 1958)

(a) 2D or layer-by-layer  
(Frank - Van der Merwe)



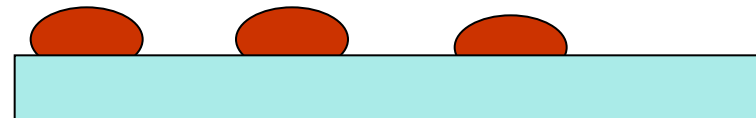
$$\Delta\gamma = \gamma_o + \gamma_i - \gamma_s < 0$$

(b) 2D followed  
by 3D islanding  
(Stranski - Krastanov)



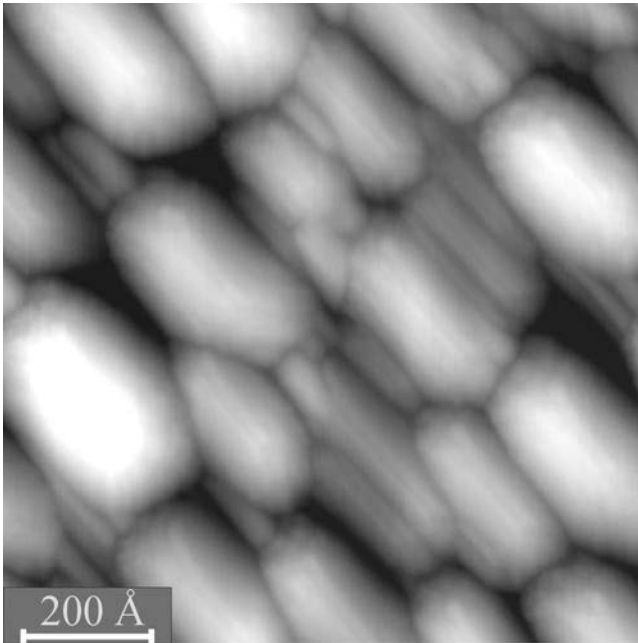
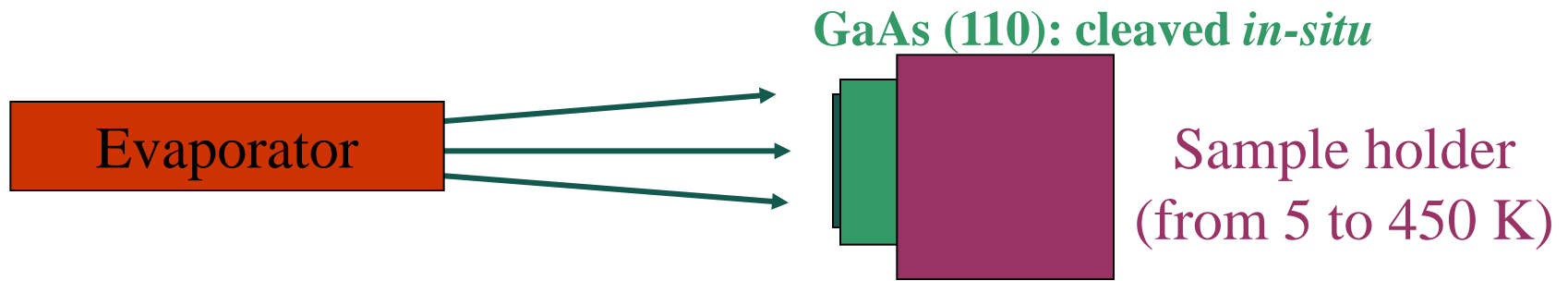
$$\Delta\gamma \sim 0$$

(c) 3D islanding  
(Volmer - Weber)

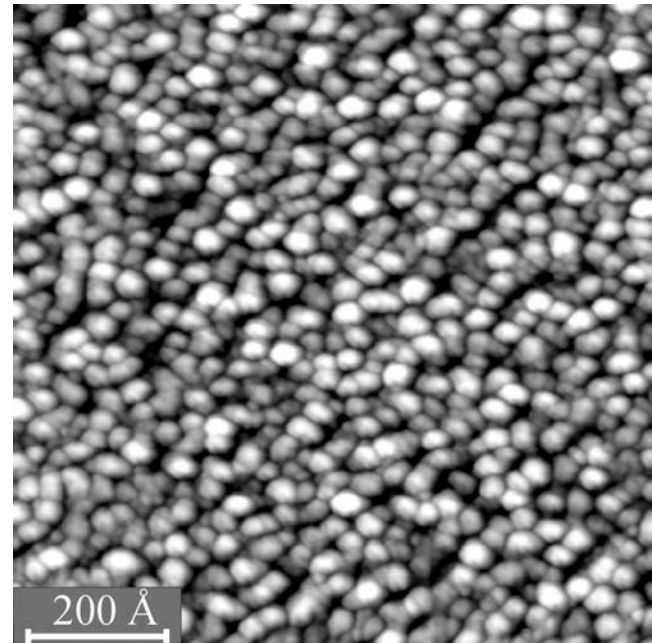


$$\Delta\gamma > 0$$

# Ag/GaAs(110): A Prototype Nonwetting System

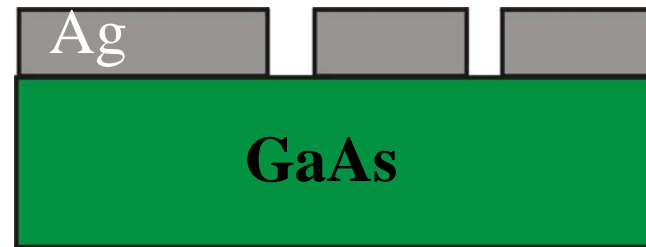
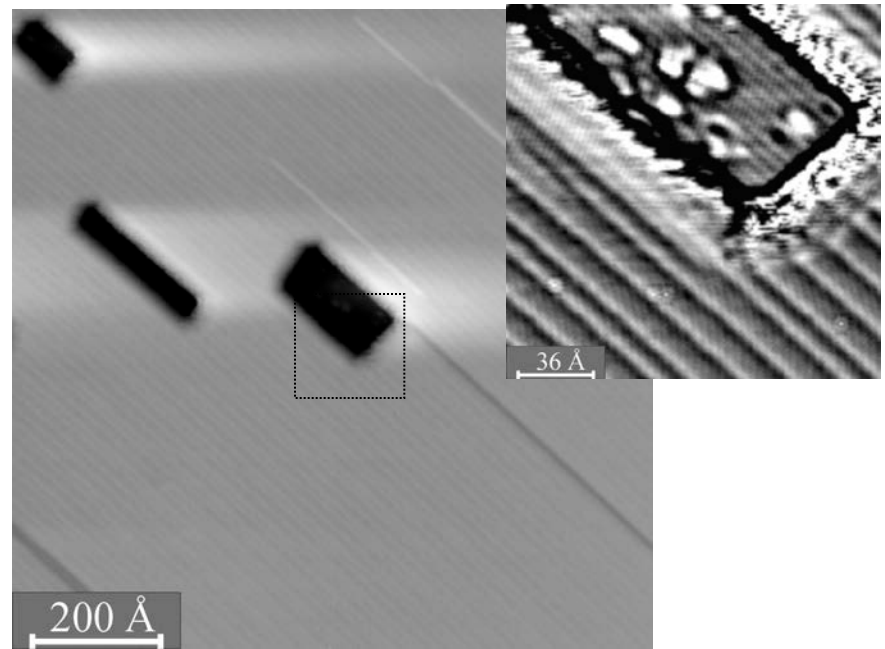
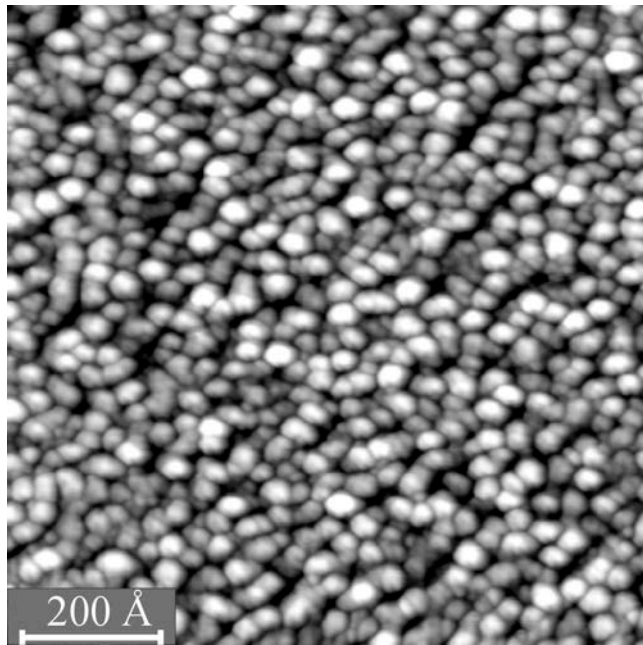


(1.5 nm deposition at 300 K)



(1.5 nm deposition at 135 K)

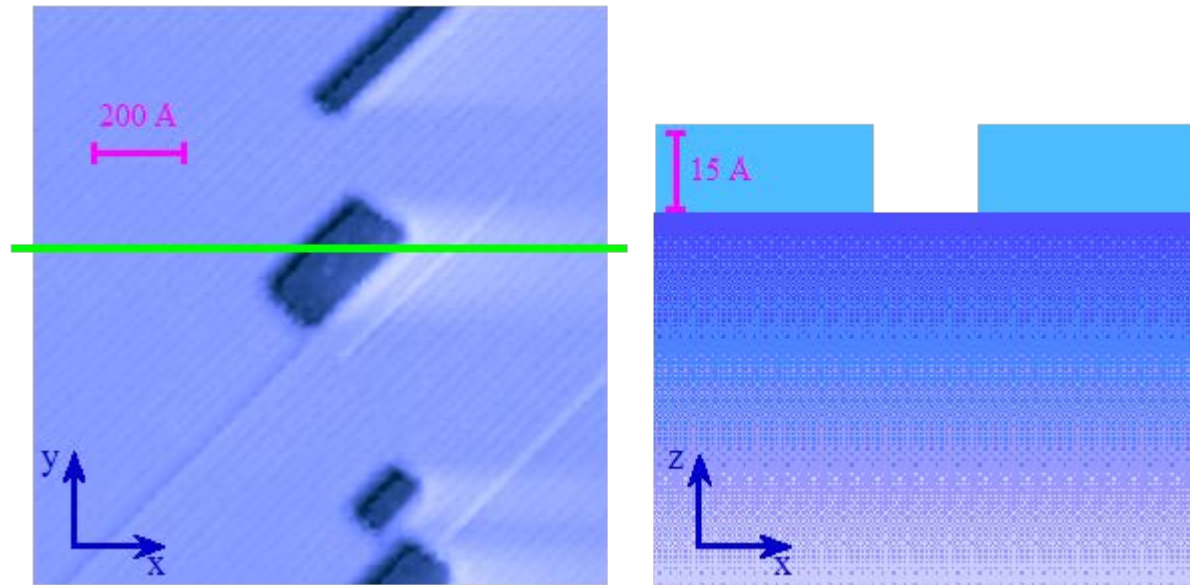
# Formation of Atomically Flat Ag films **Above** $h_c$ (Smith, Chao, Niu, Shih, Science 273, 226 (1996))



$h_c = 6 \text{ ML}$

LT deposition  $\longrightarrow$  Annealing to RT

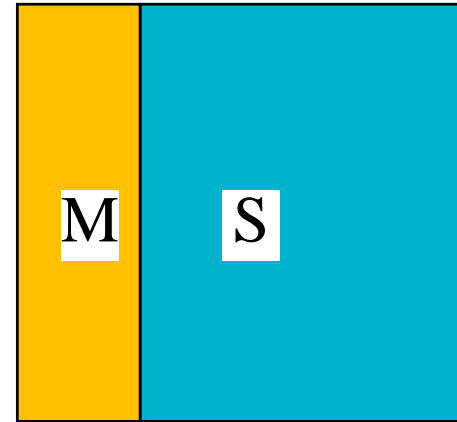
# What Defines the Critical Thickness for Ag Growth on GaAs(110)?



- ◆ Individual atomistic mechanisms are insufficient to explain this phenomenon.
- ◆ Neither due to strain.

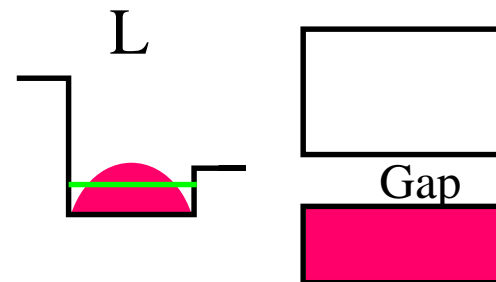
# First Conjecture:

The critical thickness is defined by the confined motion of the conduction electrons in the metallic overlayer.



From any Q.M. textbook:

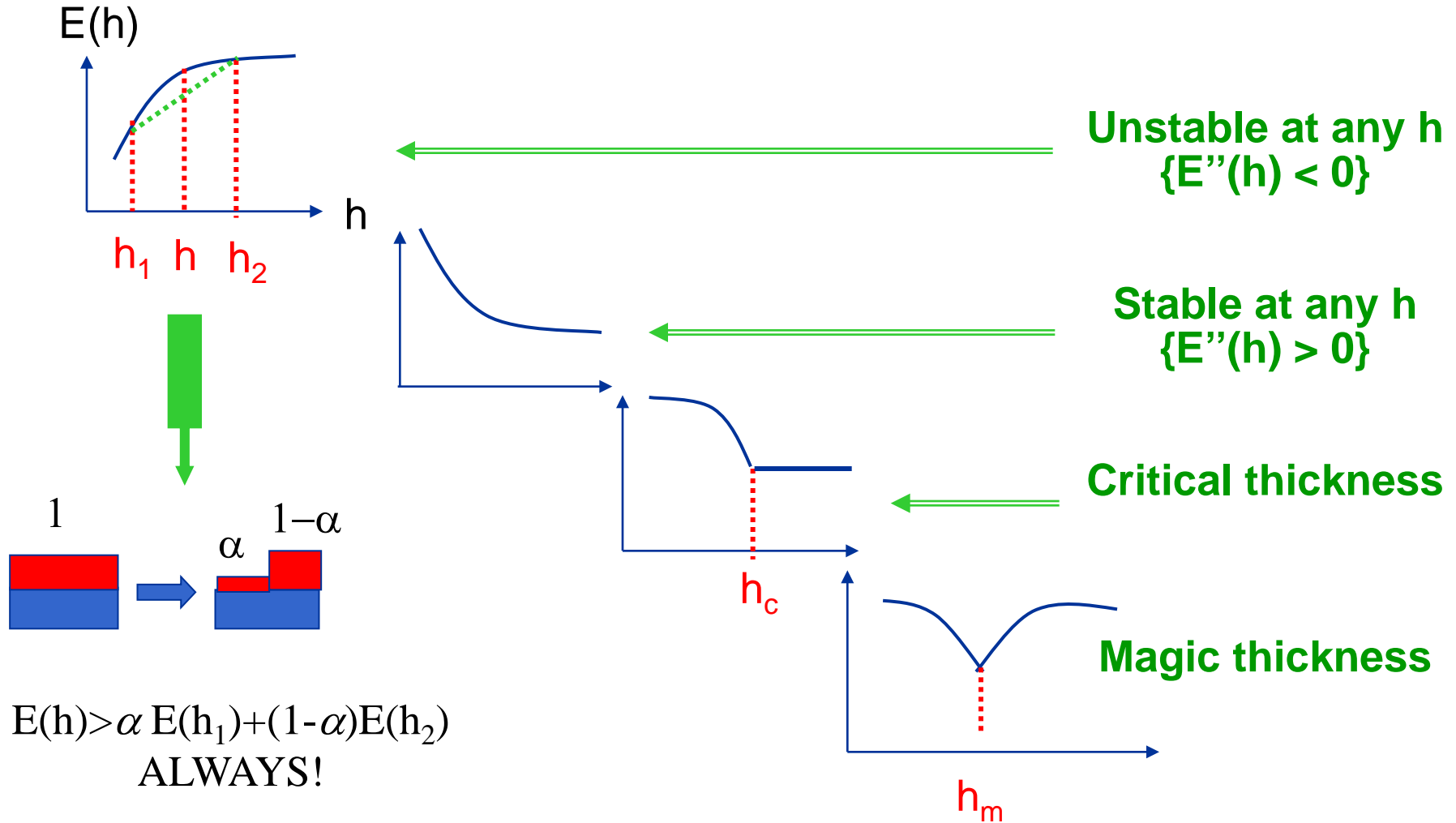
Exist the 1st bound state if  $L > L_c$





# Generic Guideline (Mechanics 101)

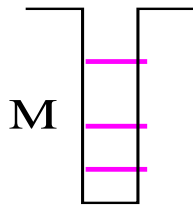
## Stability analysis of flat films with increasing thickness



# Electronic Stability of Ultrathin Ag/GaAs(110)

(Zhang, Niu, Shih, PRL 80, 1026 (1998))

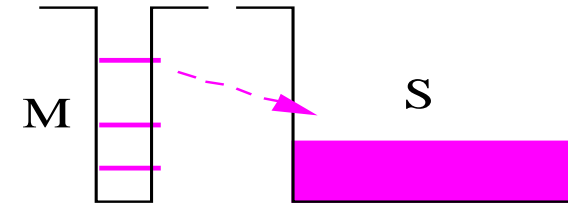
## Quantum-Size Effects



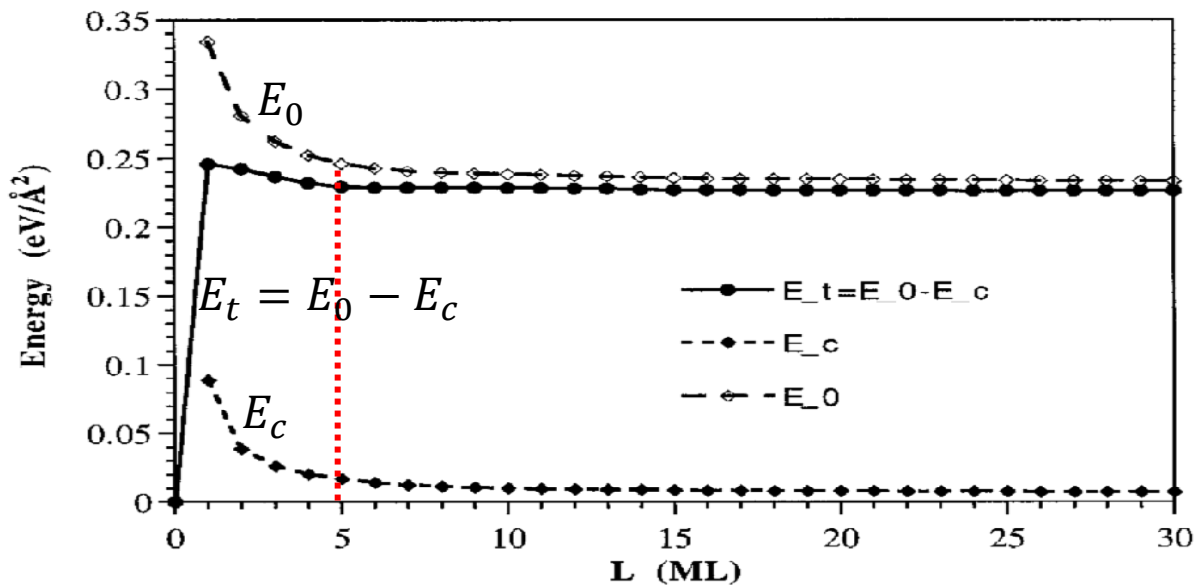
energy increase  
due to confinement



## Substrate Effects

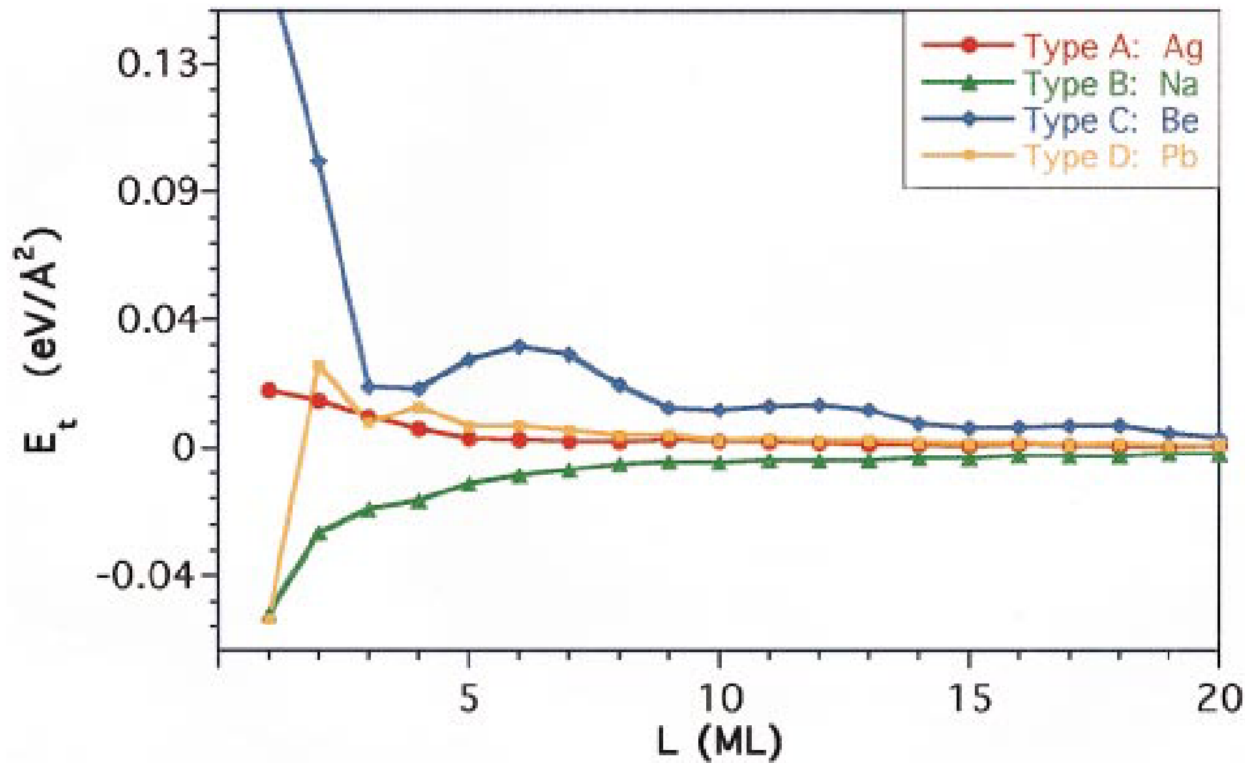


energy decrease  
due to charge spill



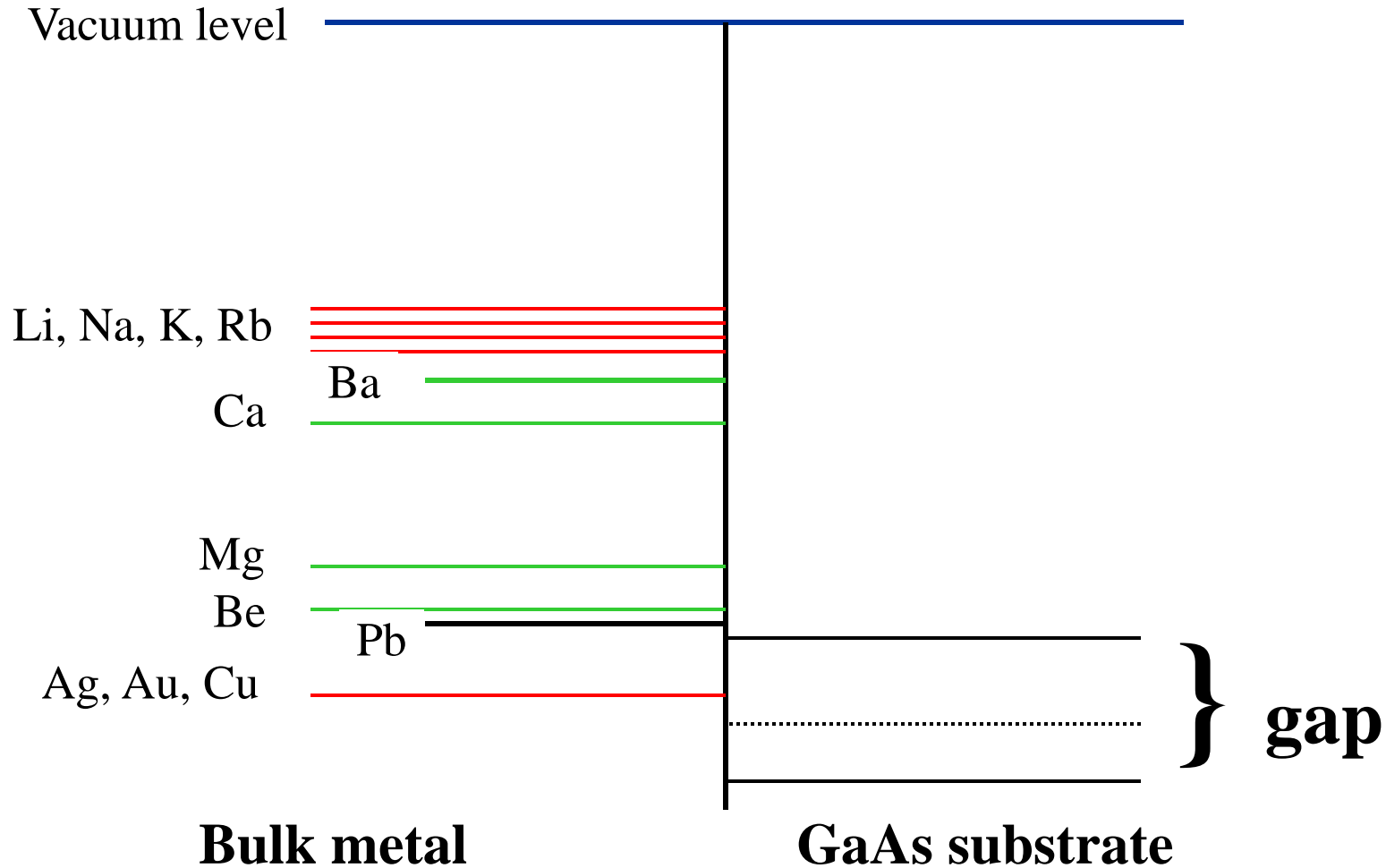
**0<sup>th</sup> order model  
(electrons in a box)**

# Electronic Stability of Other Metals on GaAs(110)

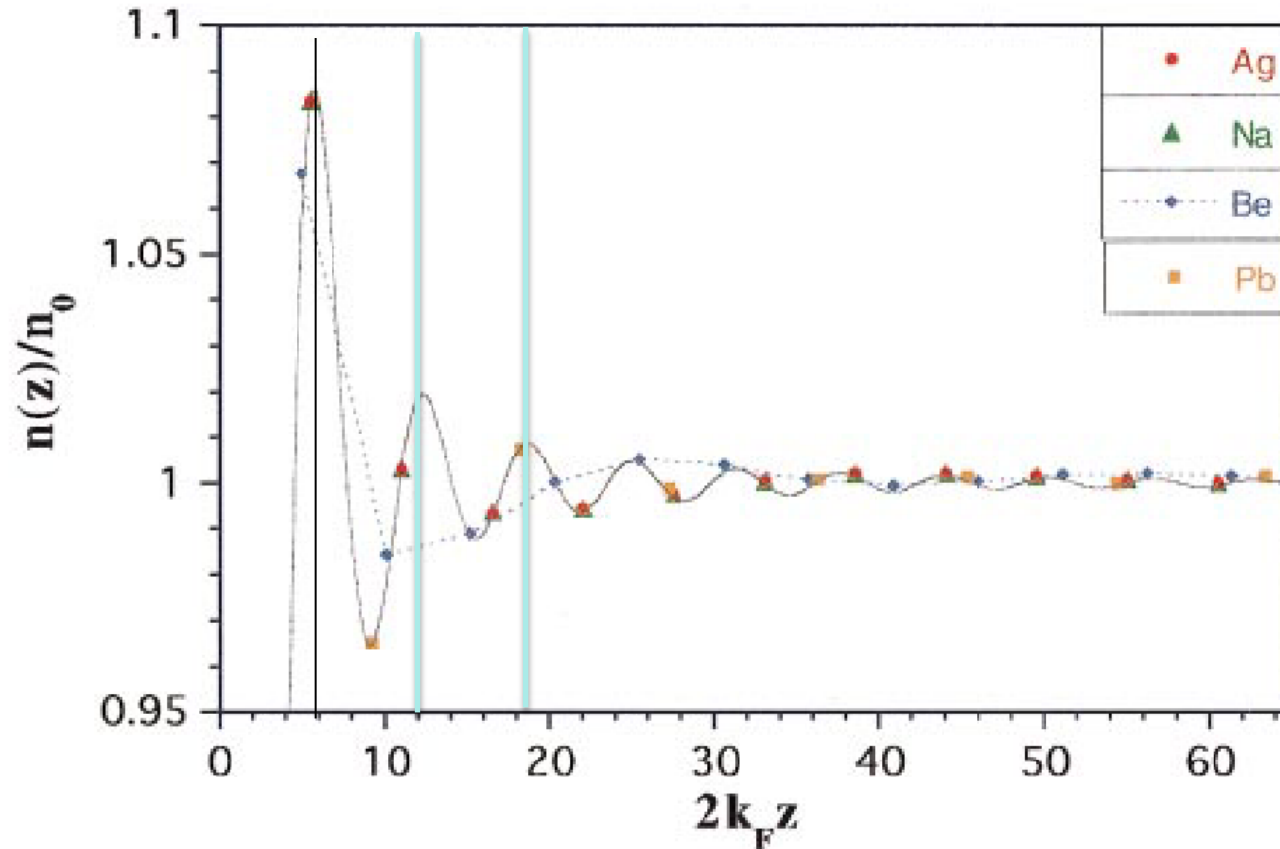


- ◆ Noble metals behave the same way if ignoring reactivity difference.
- ◆ Alkali metals behave qualitatively different.
- ◆ Multiple magic thicknesses for smooth growth of Pb & Be.

# Why Noble Metals and Alkali Metals Behave So Differently? --- Fermi Level Mismatch



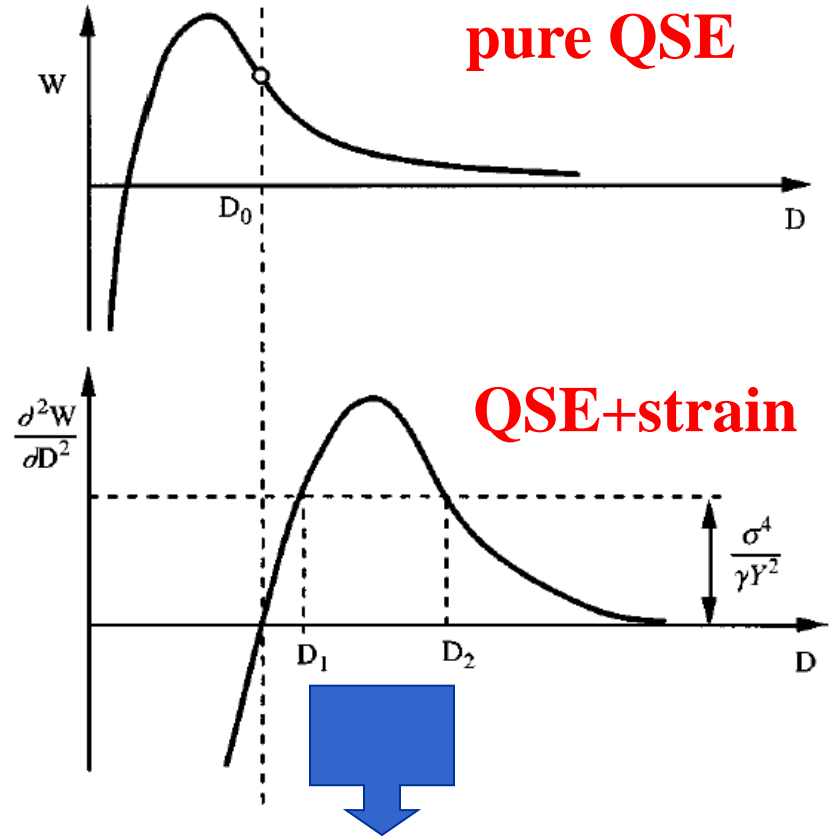
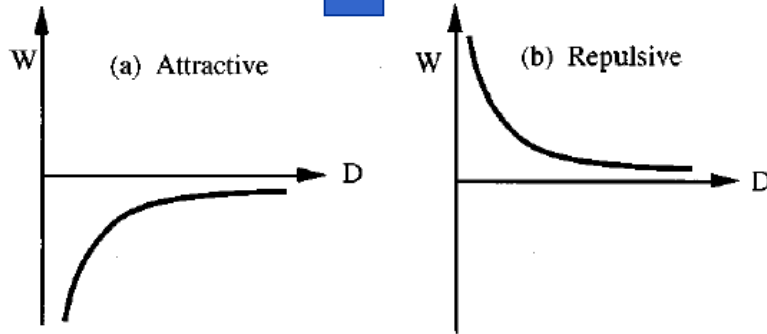
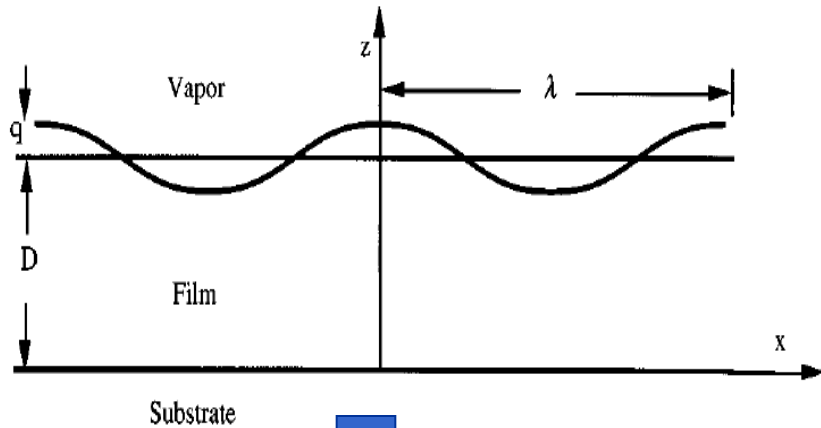
# Why Existing Magic Thickness?



**Magic thicknesses defined by commensurate length scales**  
(wavelength for electron density oscillations  
↔ intrinsic interatomic layer spacing)

# Quantum Size Effect (QSE) versus Strain

(Suo & Zhang, PRB 58, 5116 (1998))

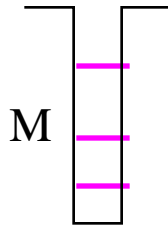


**“Window of opportunity” for smooth growth**

# Electronic Growth: Conceptual Developments

PRL 80, 1026 ('98); 80, 3582 ('98); 80, 5381 ('98); PRB 58, 5116 ('98)

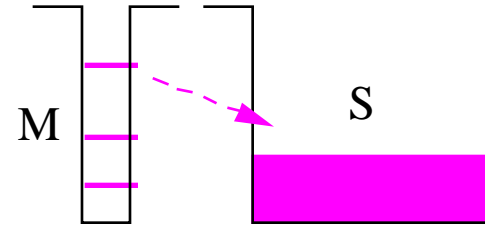
## Quantum-Size Effects



energy increase  
due to confinement



## Substrate Effects



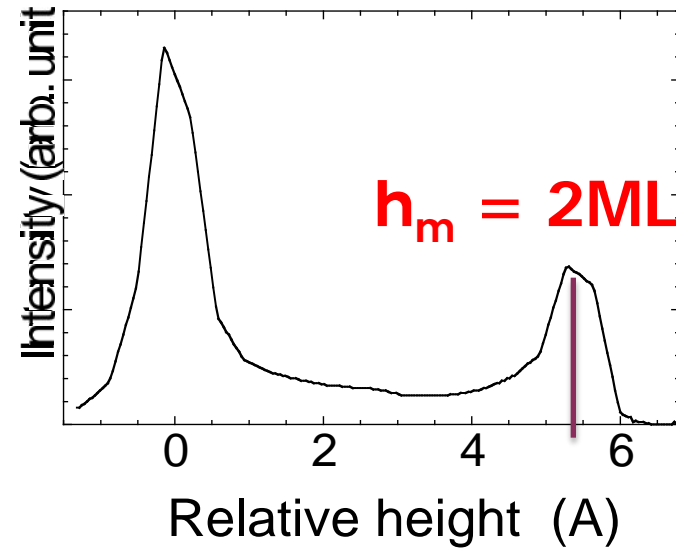
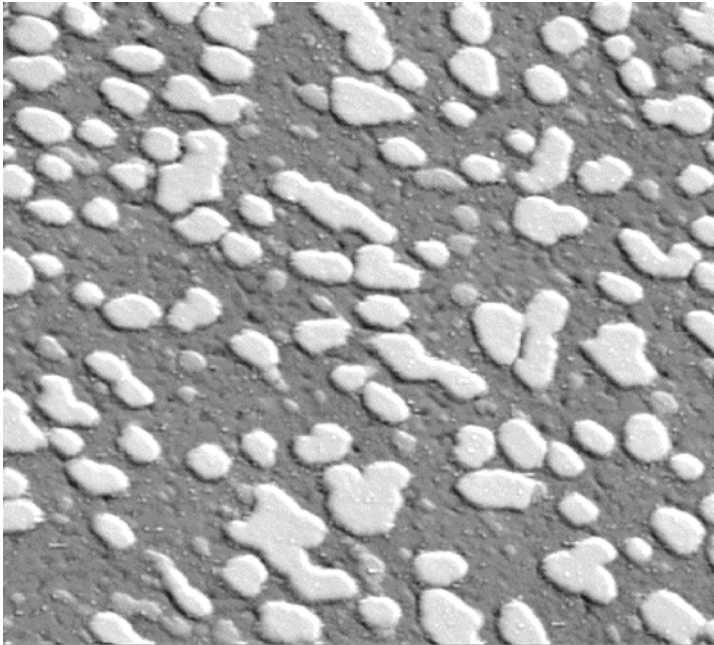
energy decrease  
due to charge spill

- Competition between quantum confinement and charge spilling leads to **critical thickness** for smooth growth.
- Commensuration between the standing wavelength and interlayer spacing determines the **magic thickness** (closed shells for 2D systems).
- In the ultrathin (quantum) regime, the electronic effects easily overwhelm the stress effects.
- **2D magic islands** may be formed in the submonolayer regime.

# Evidence for “Electronic Growth”

## Formation of Quantum Platelets in Ag/Si(111)

Gavioli, Kimberlin, Tringides, Wendelken, Zhang, PRL ('99)



**Low-T deposition, followed by annealing**

Resistivity measurement: a bad metal out of a good conductor.



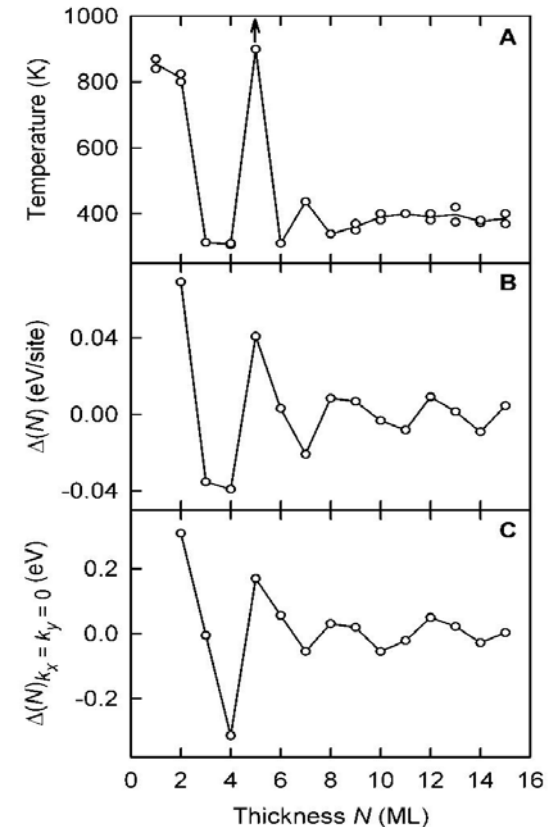
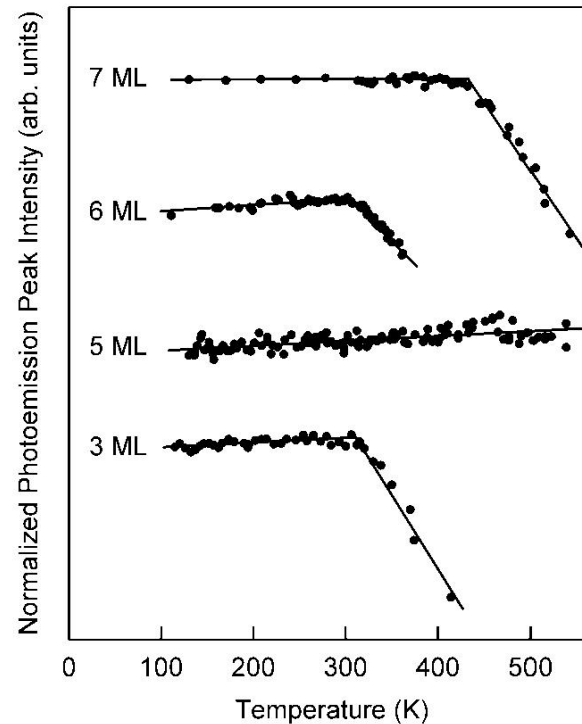
# Evidence for "Electronic Growth"

## Quantum Electronic Stability of Atomically Uniform Films

Luh, Miller, Paggel, Chou, Chiang, Science ('01)

**Ag-on-Fe(100):**  
A New Class of Systems

**"Shell Structures"**  
Science (2001)

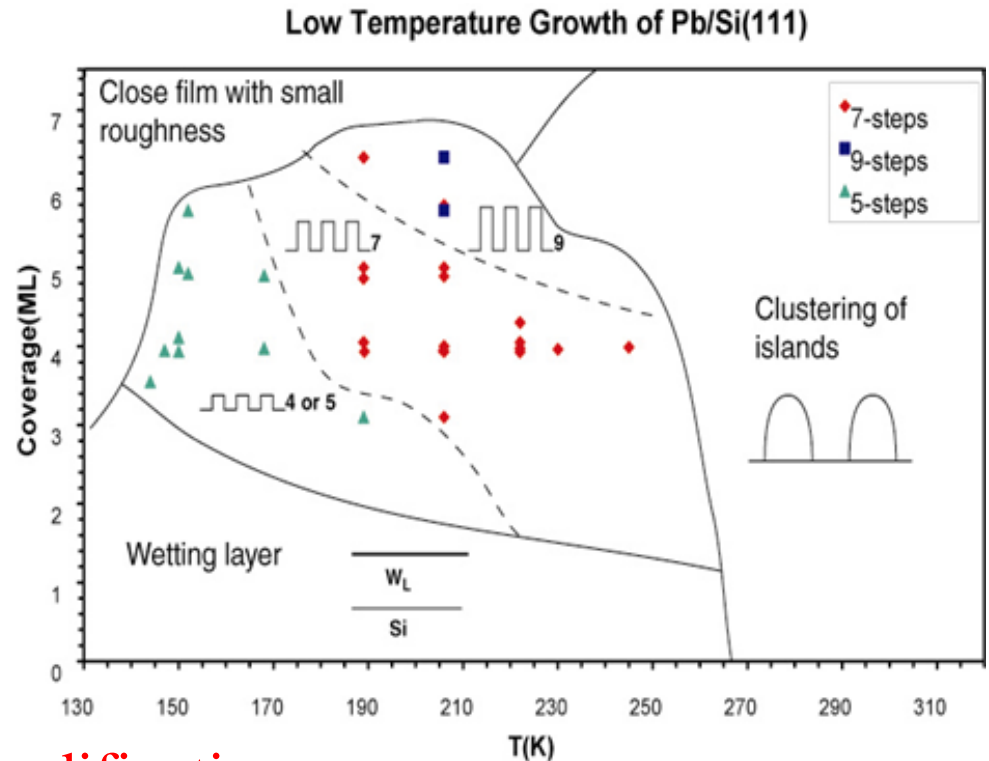
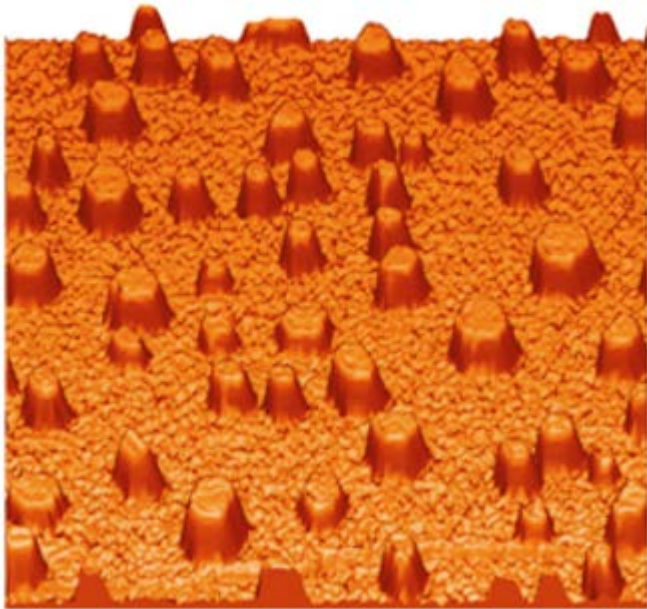


**Film with  $h=5$  ML too stable to be destroyed!**

# Validation of “Electronic Growth”:

## Thickness Tuning of Quantum Platelets in Pb/Si(111)

(Yeh, Berbil-Bautista, Wang, Ho, Tringides, PRL (2000))



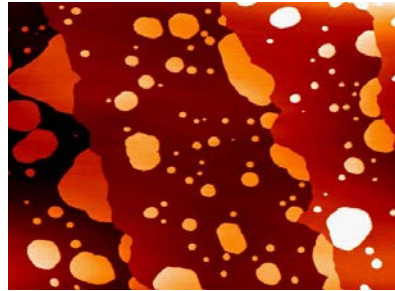
“7”  $\rightarrow$  “5” via interface modification:



# Bilayer-by-bilayer growth of Pb/Si(111)



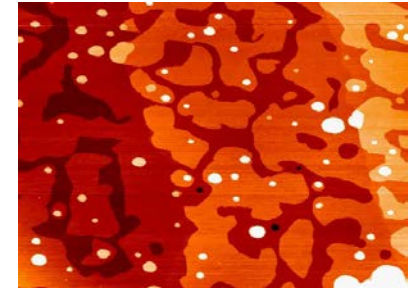
5 & 7 ML



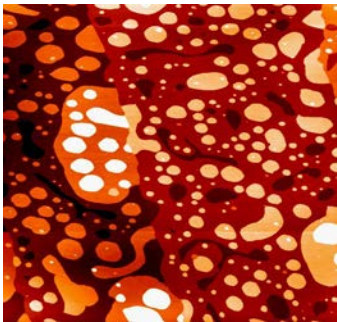
7 & 9 ML



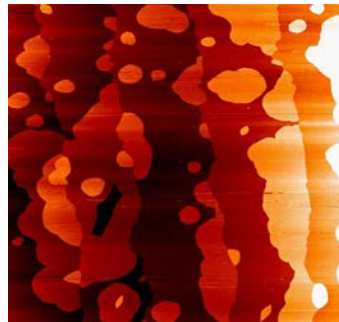
9 & 11 ML



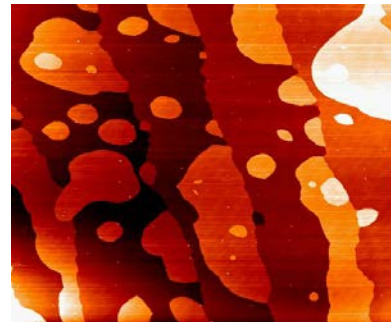
13 & 14 ML



16 & 18 ML



18 & 20 ML



20 & 22 ML



22 & 25 ML

(Ozer, Jia, Wu, Zhang, & Weitering, *PRB* 72, 113409, 2005)

Stable layers: 4-5-7-9-11-13-14-16-18-20-22...25 ML

# QSE: “Beating Effect”

$$E_s = A \frac{\cos[2k_f(N + \Delta N)t_0]}{(N + \Delta N)^\alpha} + B$$

$$E_{lattice} = A_0 \cos(2k_{BZ}t_0 + \varphi)$$

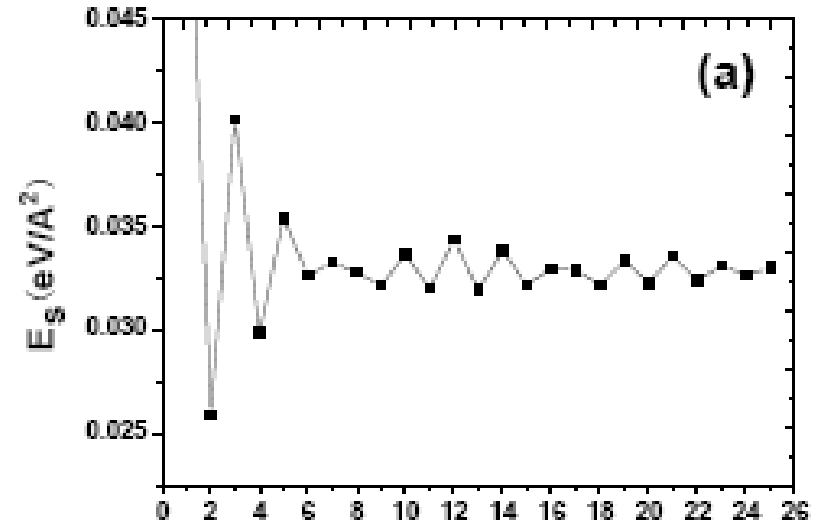


FIG. 5: (a) Surface energies of free standing Pb films.

$$k_f = 1.59 A^{-1}; t_0 = 2.84 A$$

$$k_{BZ} = \frac{\pi}{t_0}$$

$$2.07 \times t_0 = 3 \times \frac{\lambda_f}{2}$$

**slight mismatch**

$$\lambda_{beating} = \frac{\pi}{3k_{BZ} - 2k_f}$$

$$\lambda_{beating} = 9.6 ML$$

with  $k_f \uparrow$ ,  $\lambda_{beating} \uparrow$

# Quantum Tuning of Functional Properties

---

## ■ Philosophy:

**Film thickness  $L \Rightarrow$  density of states  $\rho(E_F)$   
 $\Rightarrow$  many properties**

## ■ Examples of properties:

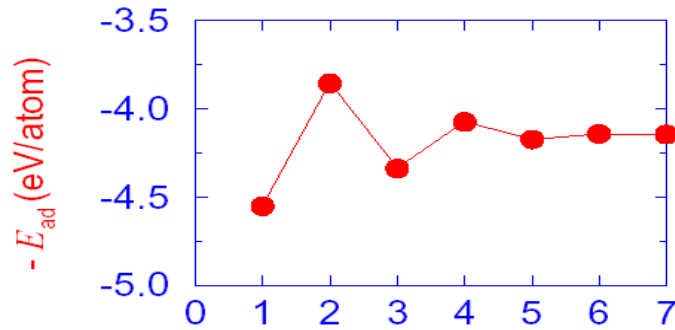
- lattice relaxation
- work function
- *electrical conductivity*
- superconductivity
- adatom diffusivity
- chemical reaction rates
- electronic friction/quantum tribology
- ...

# Sb/GaAs(110): From Structures to Transport

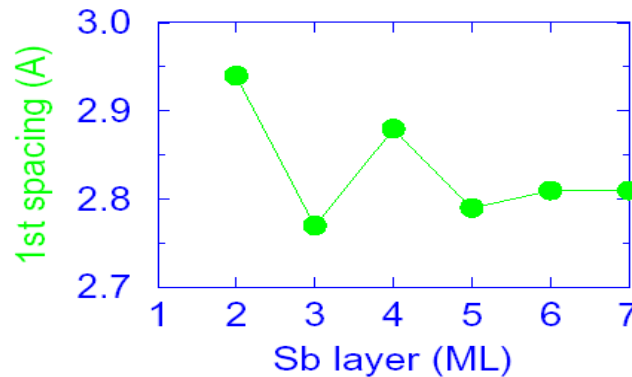
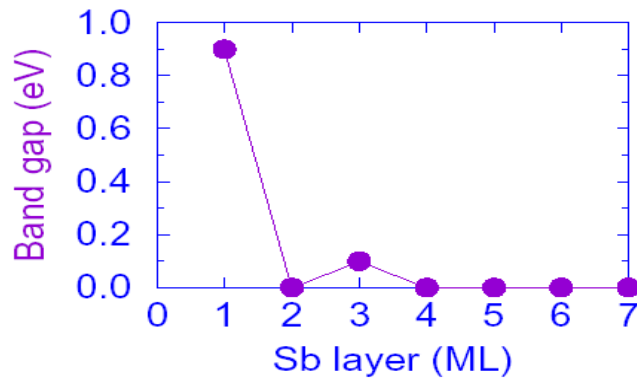
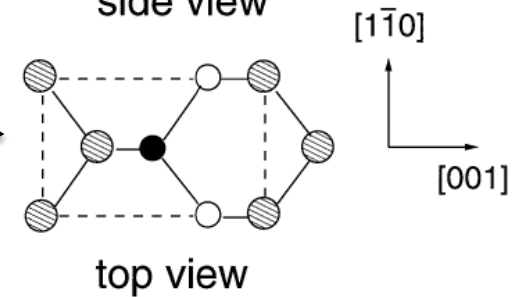
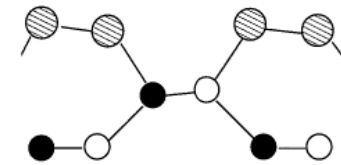
(Cho, Niu, Zhang, PRL 80, 3582 (1998); & Physical Review Focus)

## Signature for quantum-size growth

$$E_{ad} = [E(\theta_{Sb} = n - 1 \text{ ML}) - E(\theta_{Sb} = n \text{ ML}) + 4E_{a,Sb}]/4$$



○ Sb ○ Ga ● As



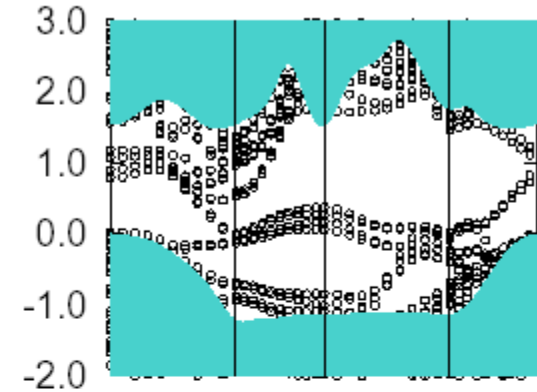
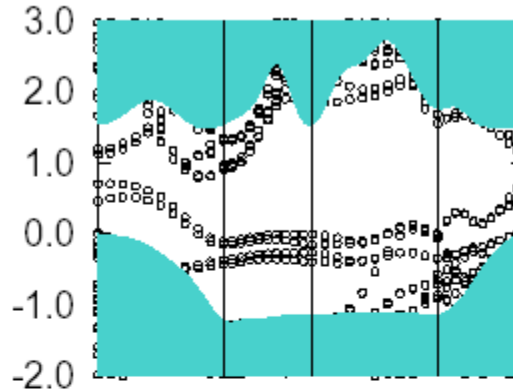
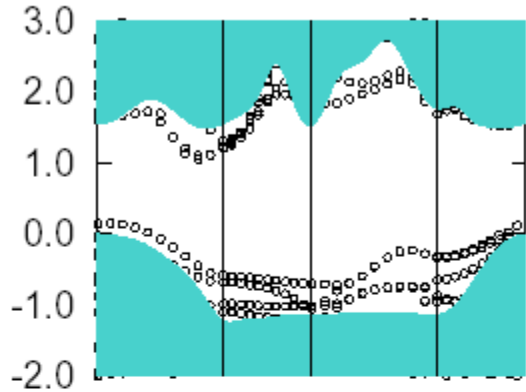
	$d_{01}$
1 ML	2.39
2 ML	2.54
3 ML	2.41
4 ML	2.44
5 ML	2.43
6 ML	2.44
7 ML	2.43

# Sb/GaAs(110): Gap Evolution

1 ML

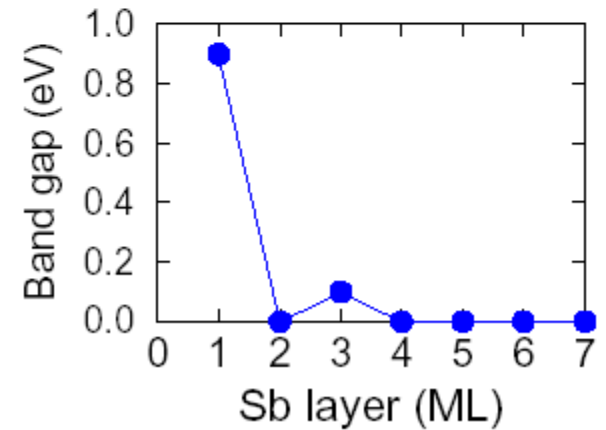
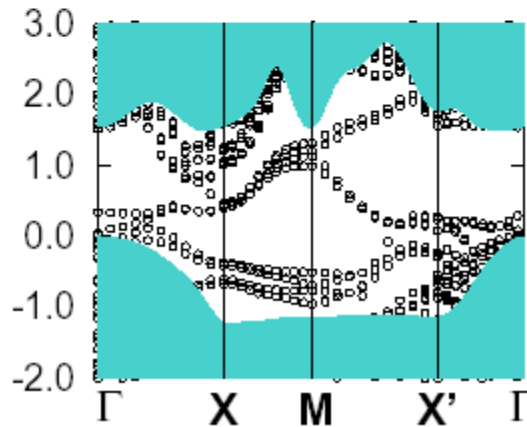
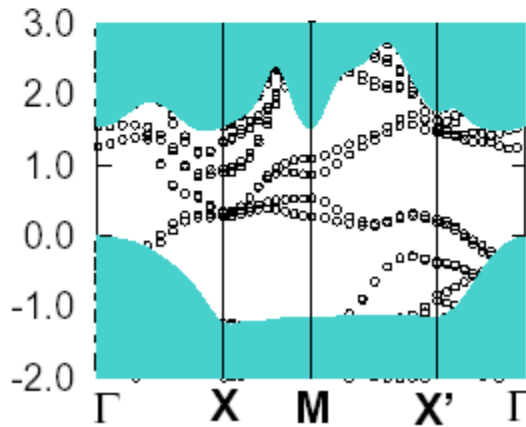
3 ML

5 ML



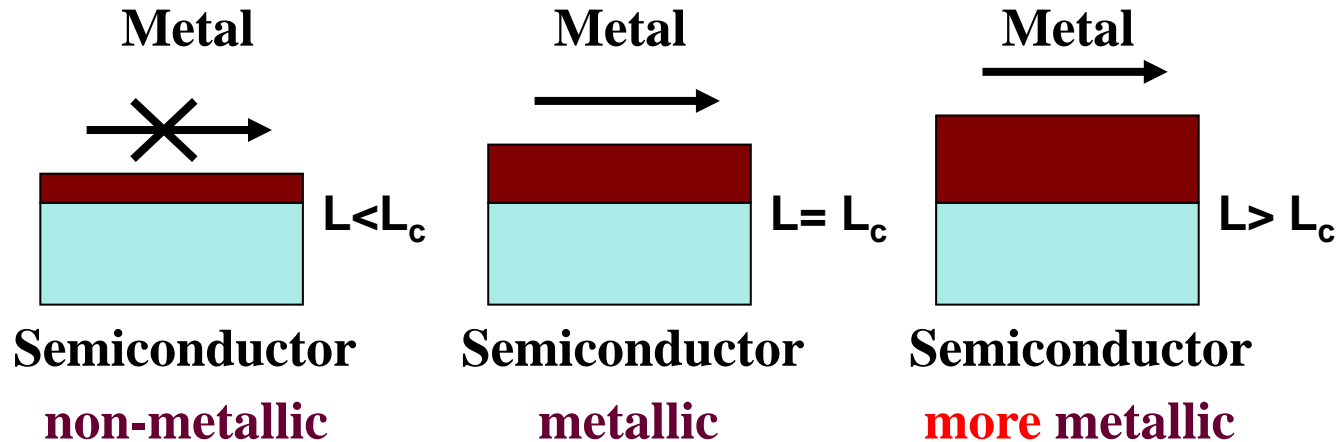
2 ML

4 ML

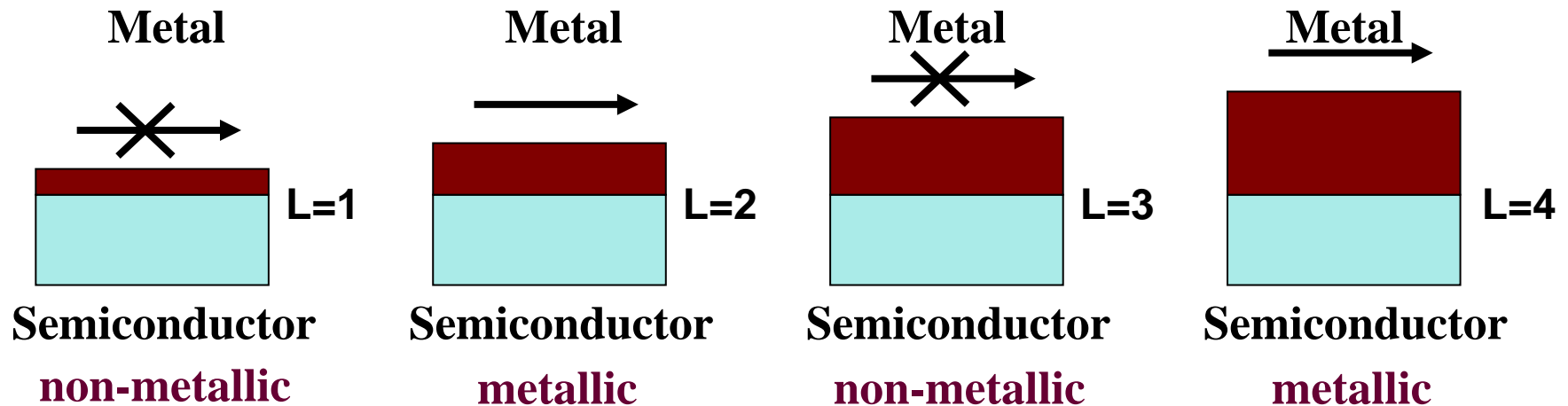


# Oscillatory Nonmetal-Metal Transitions

## Traditional Belief:

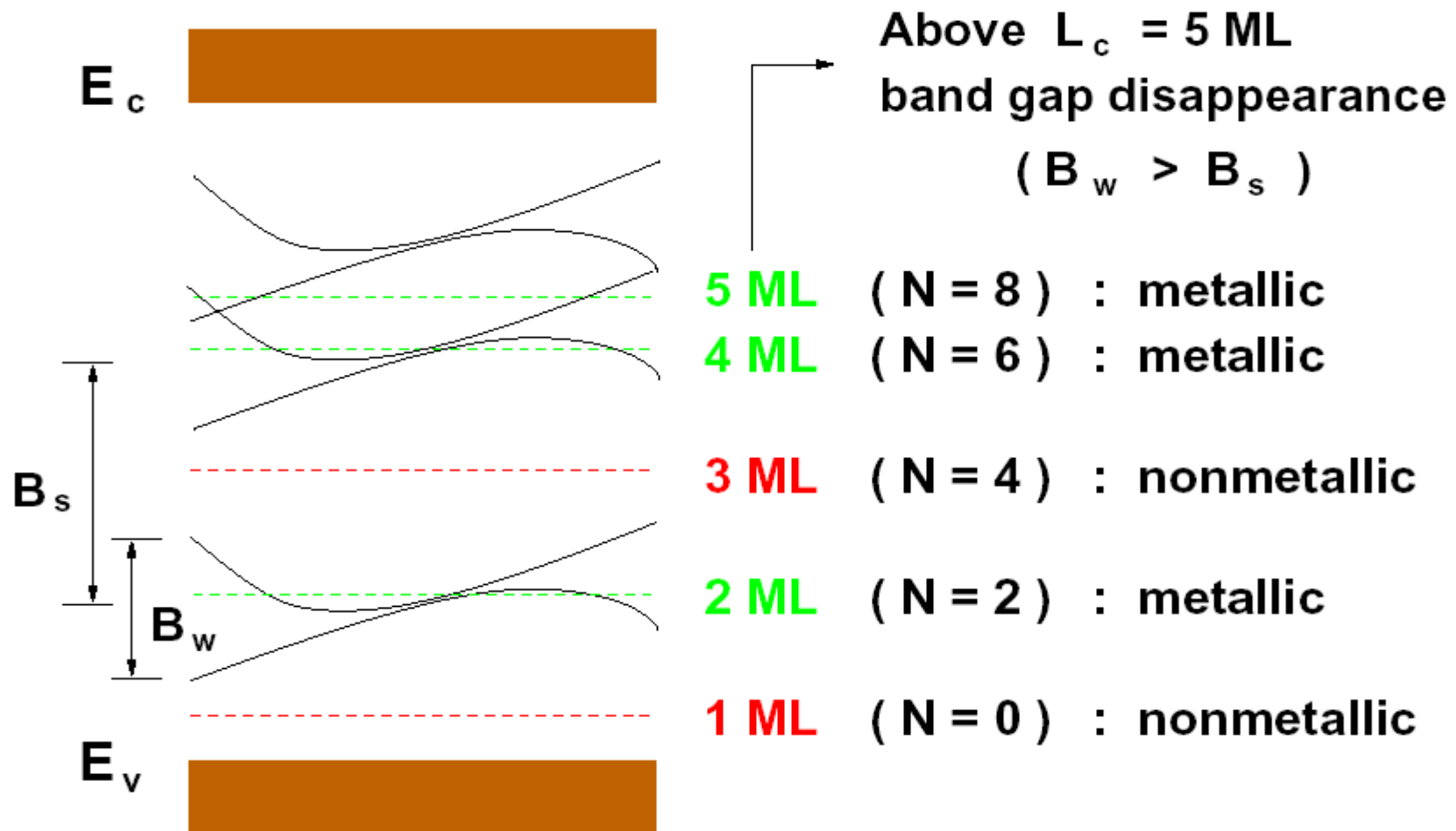


## New Finding:





# Schematic diagram of oscillatory NM-M transitions



- The adsorption energy per layer oscillates with the overlayer thickness, making stable flat films at 1, 3, and 5 ML coverages.
- For films at different thicknesses, there exist strong oscillations in the topmost interlayer spacings.
- There are oscillatory nonmetal-metal transitions as the film thickness increases.

# Quantum Tuning of Functional Properties

---

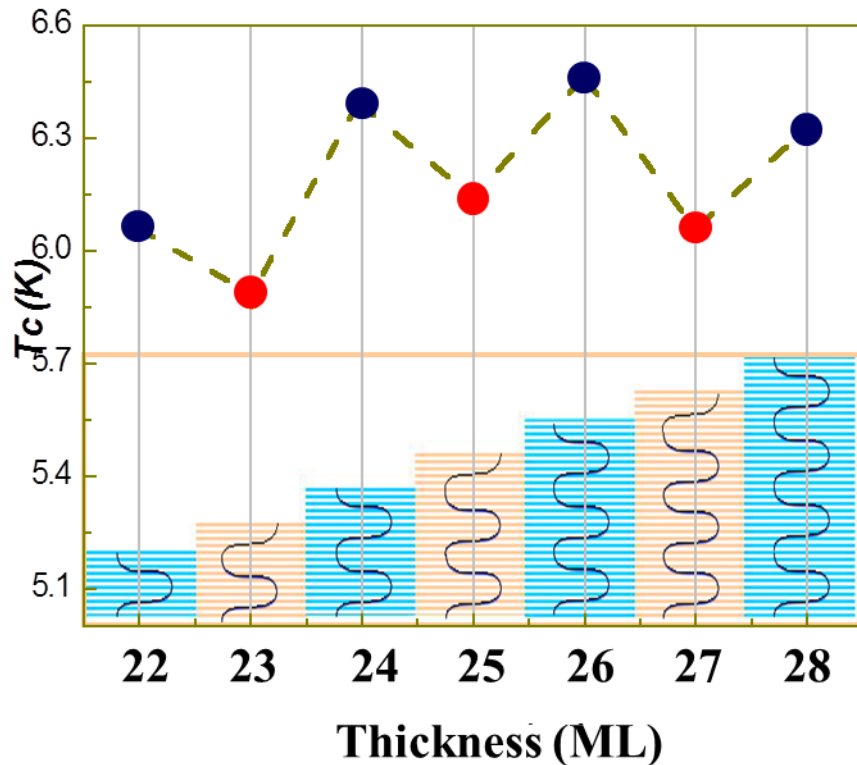
## ■ Philosophy:

**Film thickness  $L \Rightarrow$  density of states  $\rho(E_F)$   
 $\Rightarrow$  many properties**

## ■ Examples of properties:

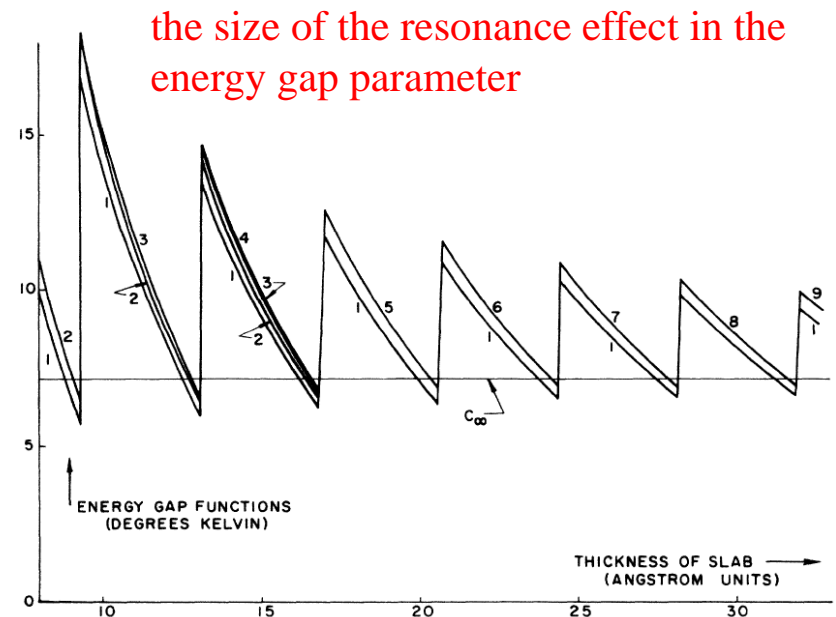
- lattice relaxation
- work function
- electrical conductivity
- ***superconductivity***
- adatom diffusivity
- chemical reaction rates
- electronic friction/quantum tribology
- ...

# Pb/Si(111): $T_c$ Oscillation vs film thickness



Blatt and Thompson, Phys. Rev. Lett. 10, 332 (1963)

Superconductor equation is solved for a slab with thickness  $a$ . Resonance effects are expected whenever an energy level (for motion perpendicular to the slab faces) passes through the Fermi surface as the thickness  $a$  is varied.

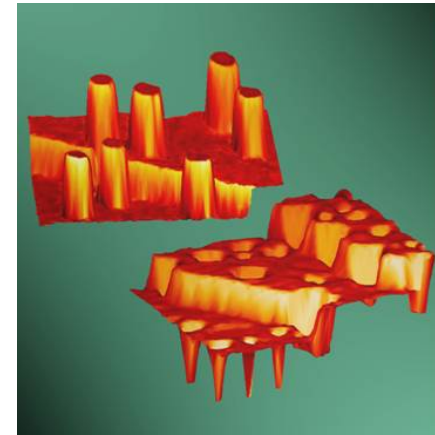
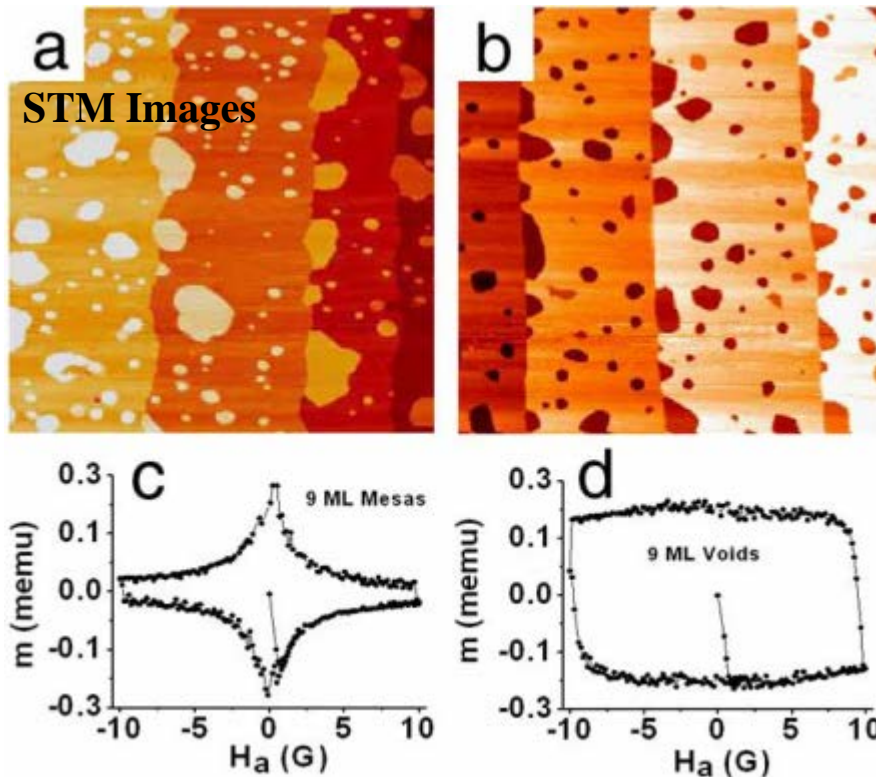


This oscillating behavior originates from the Fabry-Perot interference modes of electron de Broglie waves in the films, which modulate the electron density of states near the Fermi level and the electron-phonon coupling. Q. K. Xue, *et al.* Science 12/10/2004.

M. Ozer, Y. Jia, B. Wu, ZZ, HH Weitering, PRB 72, 113409 (2005).

## in a Soft Metal Film with Quantum Defects

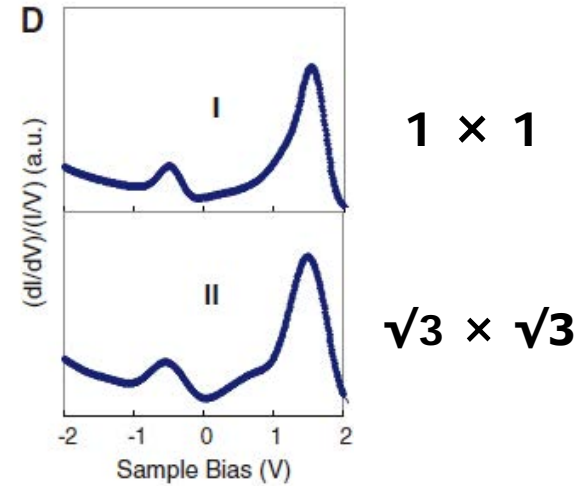
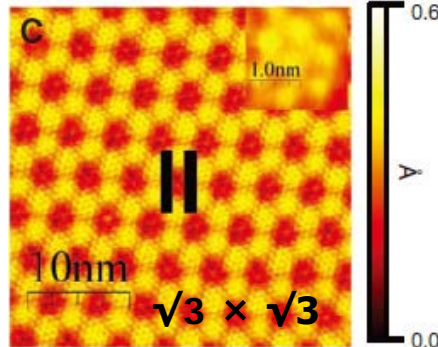
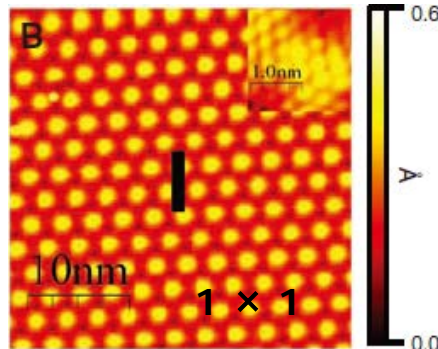
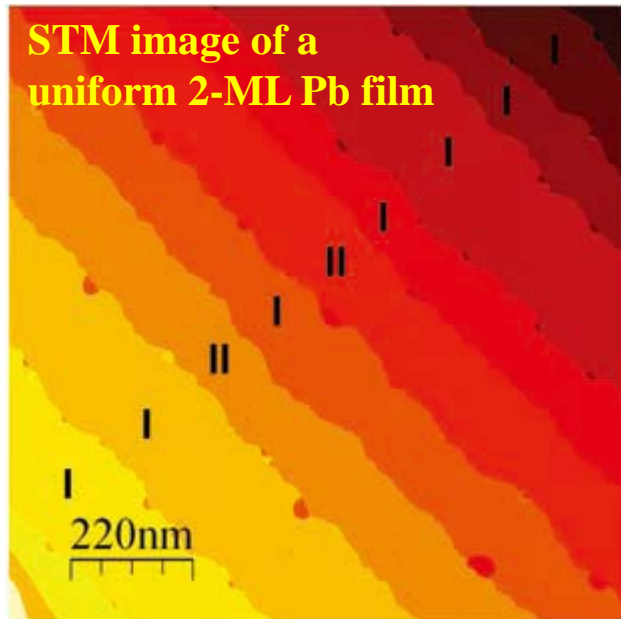
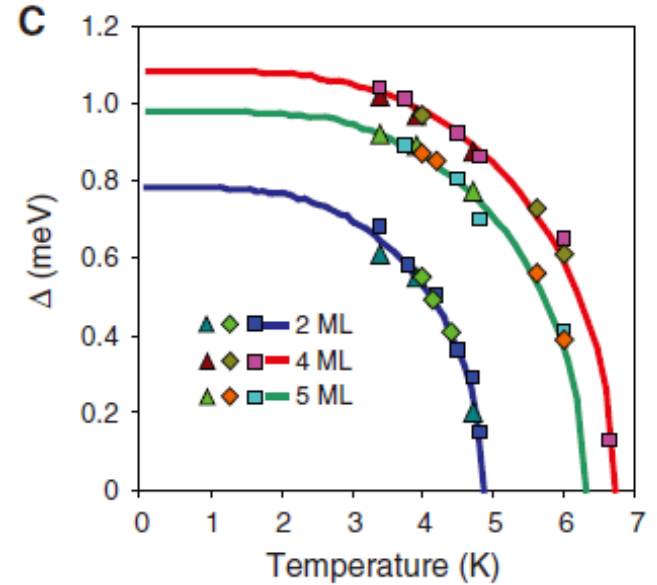
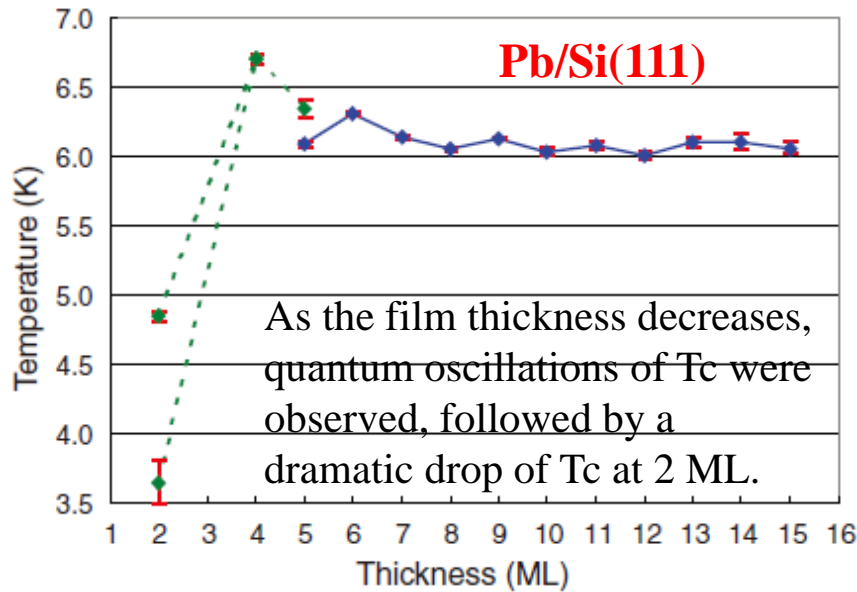
MUSTAFA M. ÖZER<sup>1</sup>, JAMES R. THOMPSON<sup>1,2</sup> AND HANNO H. WEITERING<sup>1</sup>



**DC magnetic response of these films:** Quantum voids produce “hard” hysteresis loops (d), while quantum mesas produce “soft” hysteresis loops (c).

**Superconducting state in quantum-confined geometries:** Quantum confinement of itinerant electrons in a soft metal stabilizes superconductors with vertical dimensions of only a few atomic layers. The extreme hardness of the critical state is attributed to quantum trapping of vortices.

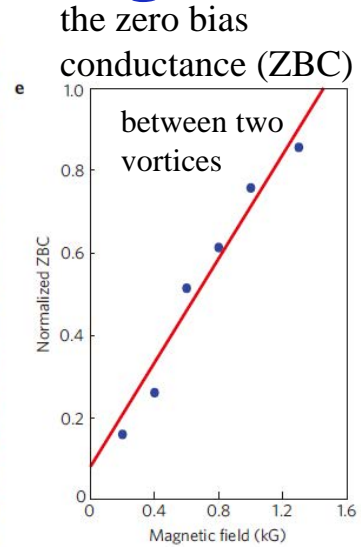
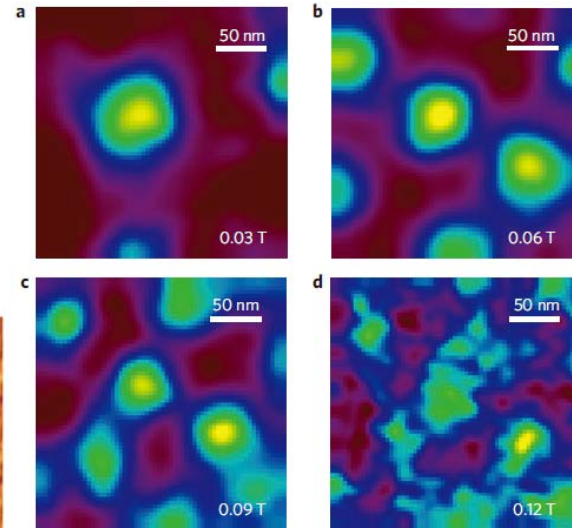
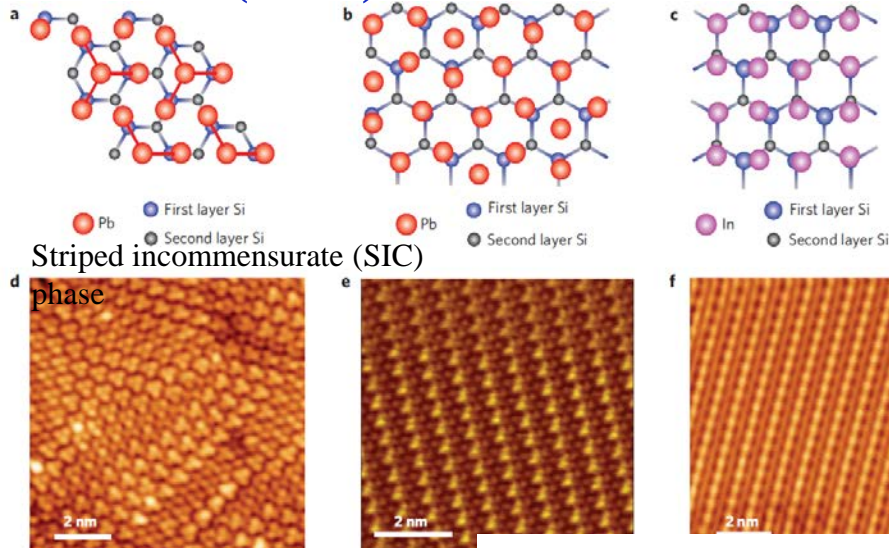
# Superconductivity at the Two-Dimensional Limit



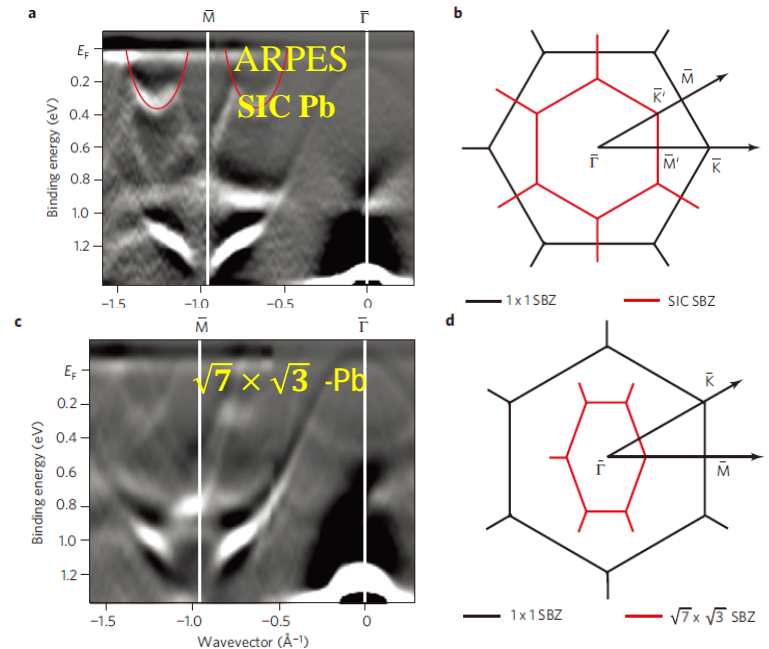
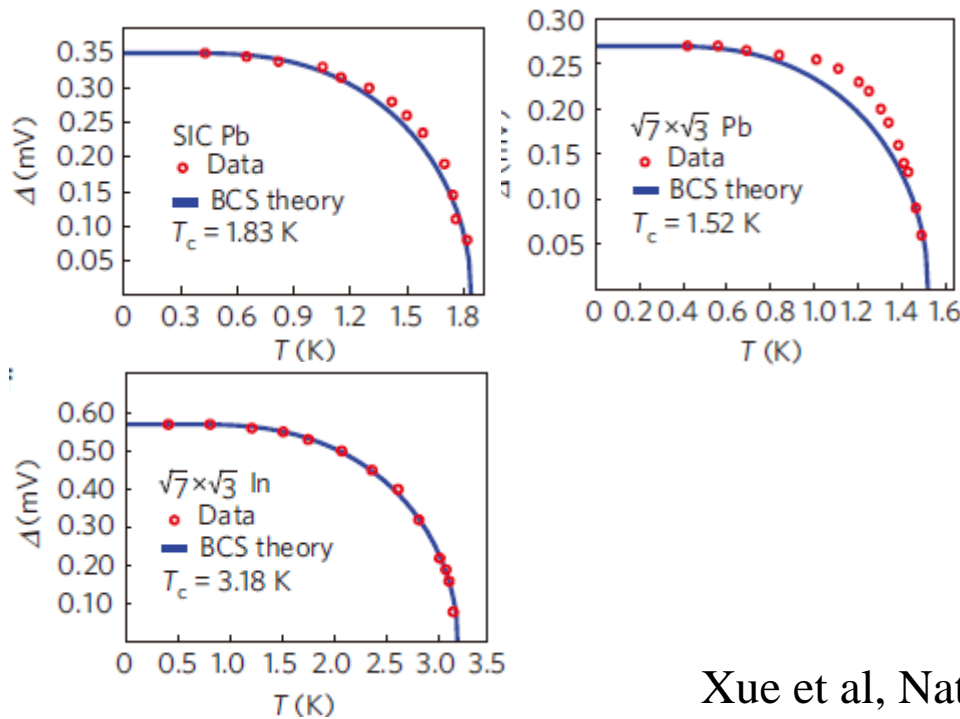
Shih et al, SCIENCE, 324, 1314 (2009)  
 Hanno H. Weiering, Chem. Phys. Chem. 2009, 10, 3183

# Superconductivity in one-atomic-layer metal films grown on Si(111)

## on Si(111)



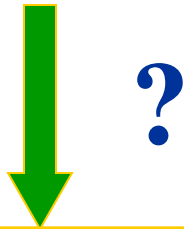
## Superconducting vortices in the SIC-Pb phase





# Quantum Alloying

Doping Bi, Ga and Hg in Pb: Pb-based alloy films



Change  $k_f$



$\lambda_{beating}$  Change



Altering Growth Mode

65.4 30 Zn	69.7 31 Ga	72.6 32 Ge	74.9 33 As	79.0 34 Se
112.4 48 Cd	114.8 49 In	118.7 50 Sn	121.8 51 Sb	127.6 52 Te
200.6 80 Hg	204.4 81 Tl	207.2 82 Pb	208.0 83 Bi	209 84 Po

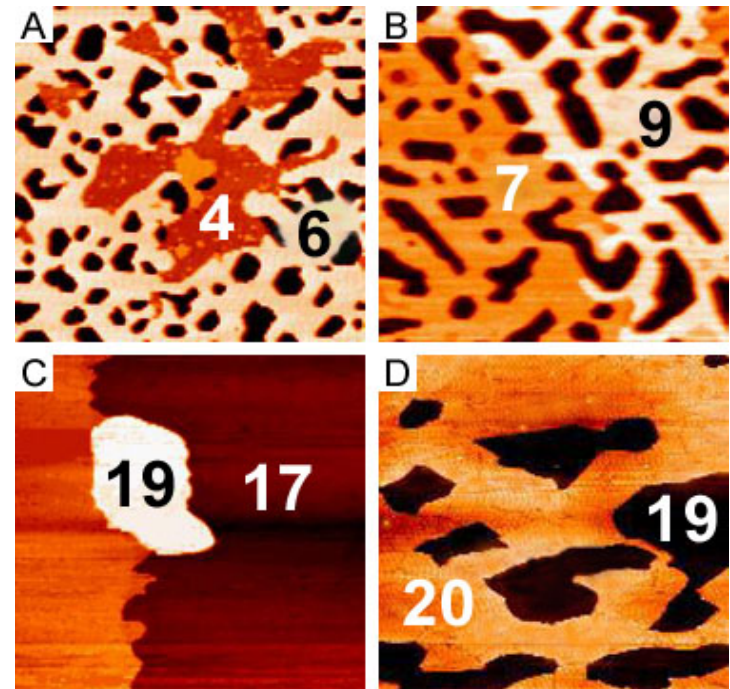
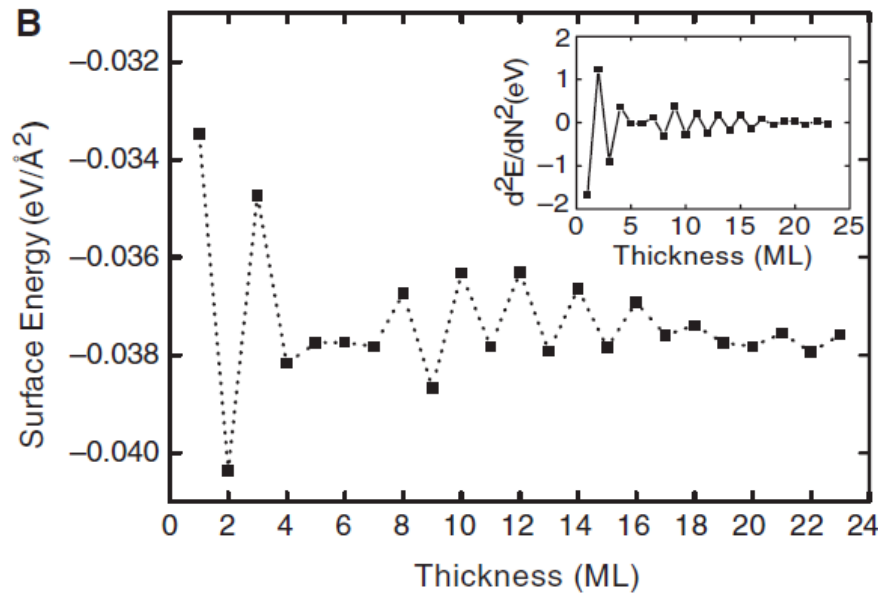


# Quantum Alloy of $\text{Pb}_{0.89}\text{Bi}_{0.11}$ on Si(111)

Ozer, Jia, Zhang, Thompson, & Weitering, Science (06/15/07)

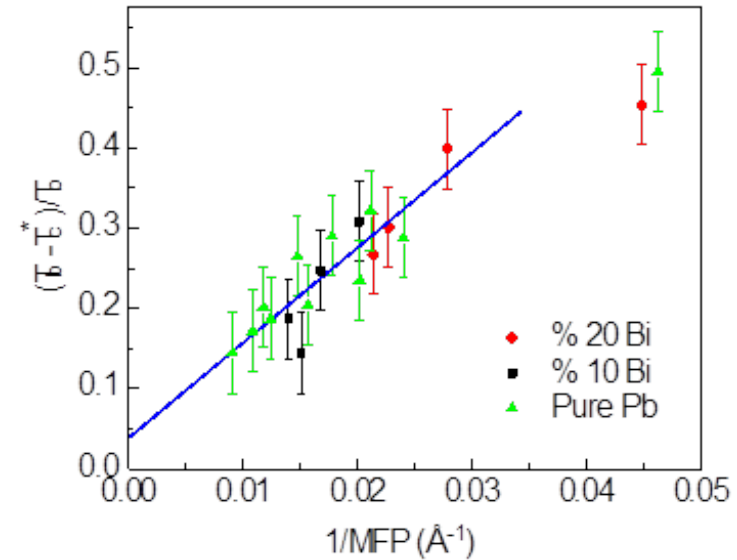
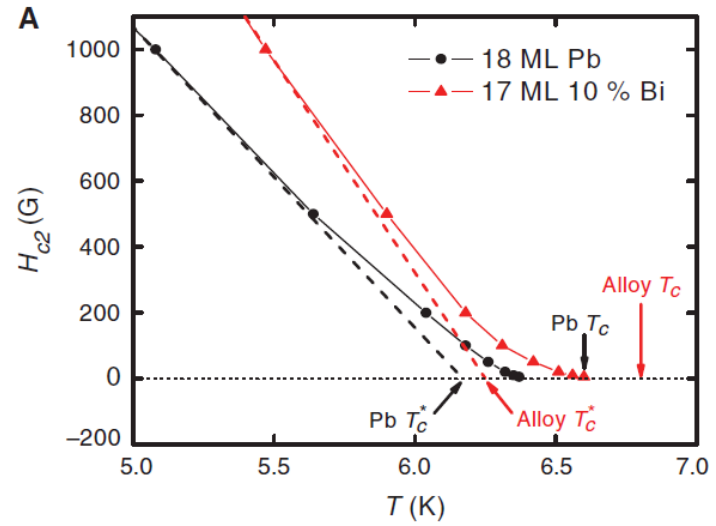
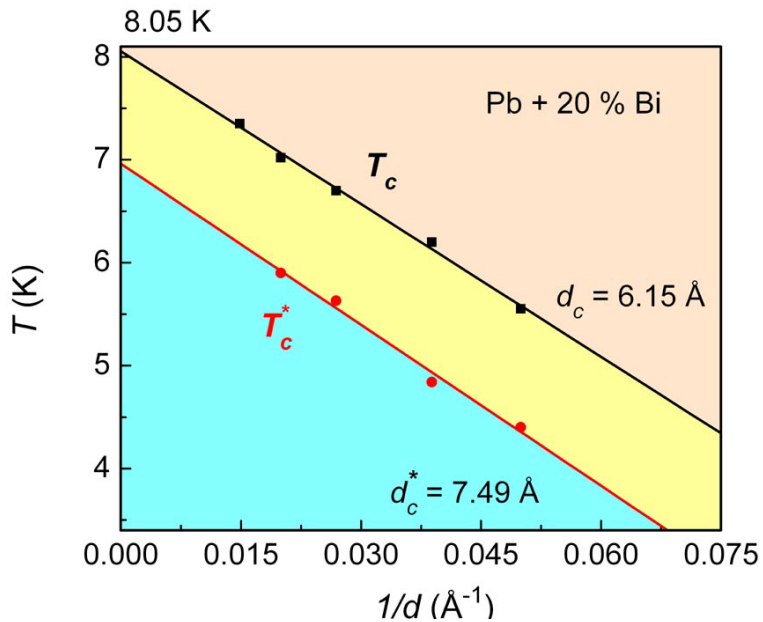
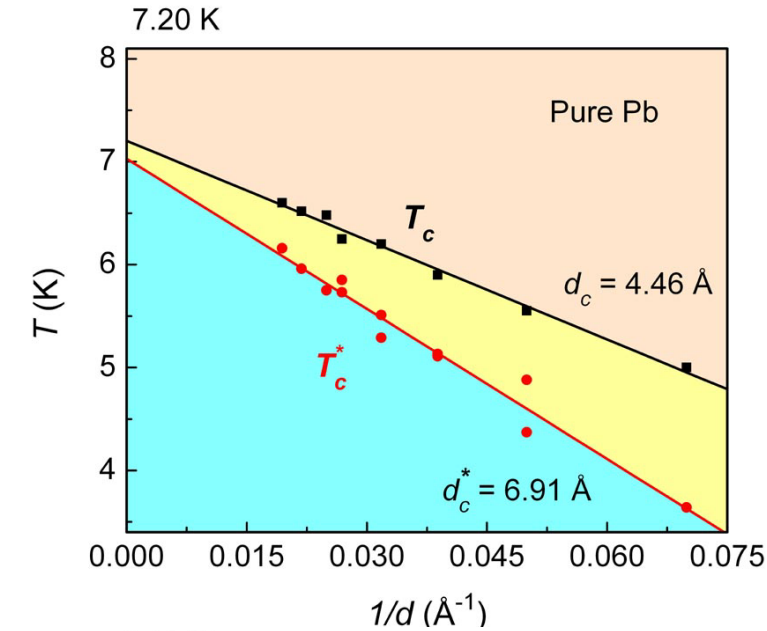
It has been shown that quantum confinement of itinerant electrons in atomically smooth ultrathin Pb films produces oscillations in the thickness-dependent film energy.

**What might be changed by adding extra electrons via bismuth alloying?**



- **Stable layer: 2-4-6-7-9-11-13-15-17-19-20-22-24-26...ML**
- **in precise agreement with experimental results.**

# Quantum Alloying



The isotropic nature of the superconductive pairing in bulk lead-bismuth alloys is altered in the quantum regime.

# Quantum Tuning of Functional Properties

---

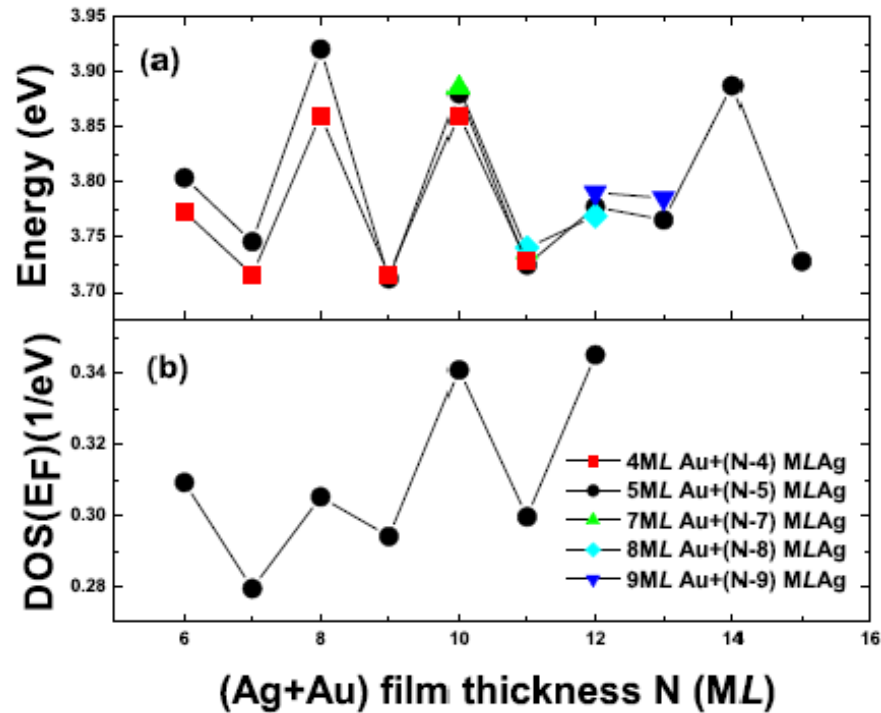
## ■ Philosophy:

**Film thickness  $L \Rightarrow$  density of states  $\rho(E_F)$   
 $\Rightarrow$  many properties**

## ■ Examples of properties:

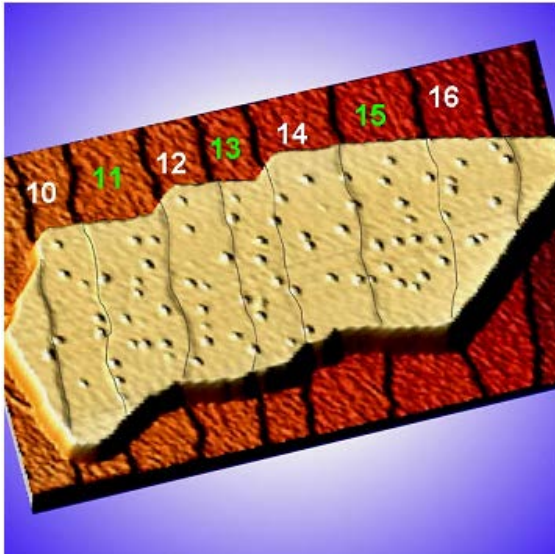
- lattice relaxation
- work function
- electrical conductivity
- superconductivity
- adatom diffusivity
- ***chemical reaction rates***
- electronic friction/quantum tribology
- ...

# Quantum Oscillations of Chemical Adsorption of O and CO on Synergetic (Au+Ag)(111) Films

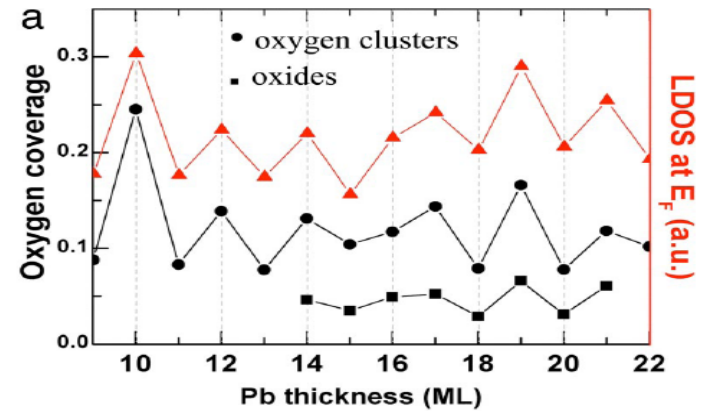
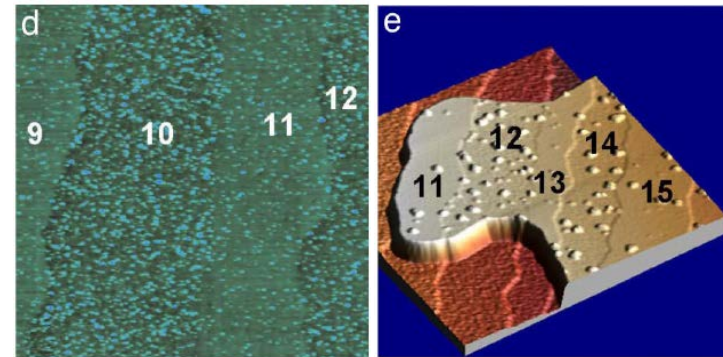


- Enhanced O or CO ( $\sim 0.2$  eV) binding on Au or Ag side
- Binding energy oscillates with the TOTAL film thickness
- Correlated oscillations in binding energy and  $\rho(E_F)$
- **DOE H initiative based on quantum metal alloys**

# Quantum Oscillations of Chemical Adsorption



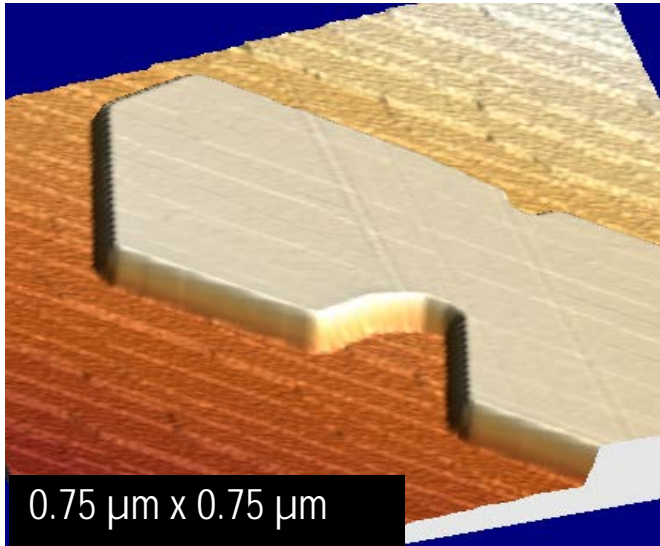
Fe on Pb/Si(111)  
Ma et al., PRL 97, 266102 (2006)



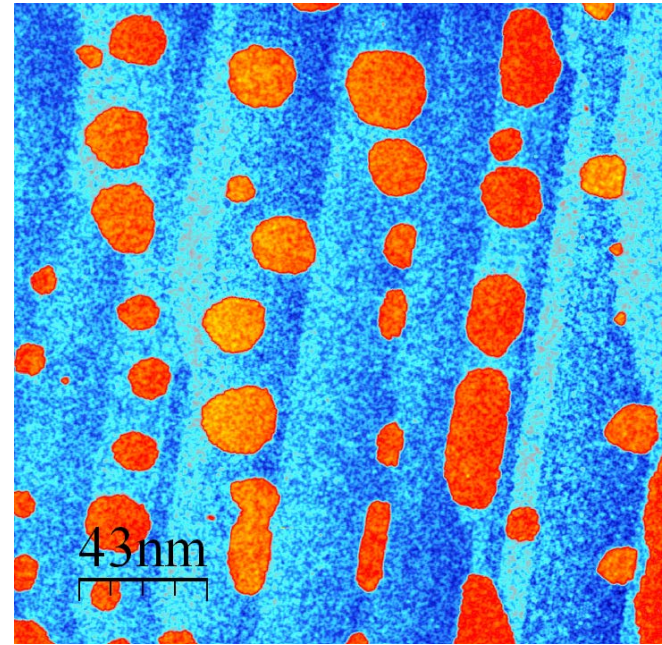
O on Pb/Si(111)  
Ma et al., PNAS 104, 920 (2007)

# Adsorbate-Induced Restructuring of Pb Nanomesa in the Quantum Regime

---

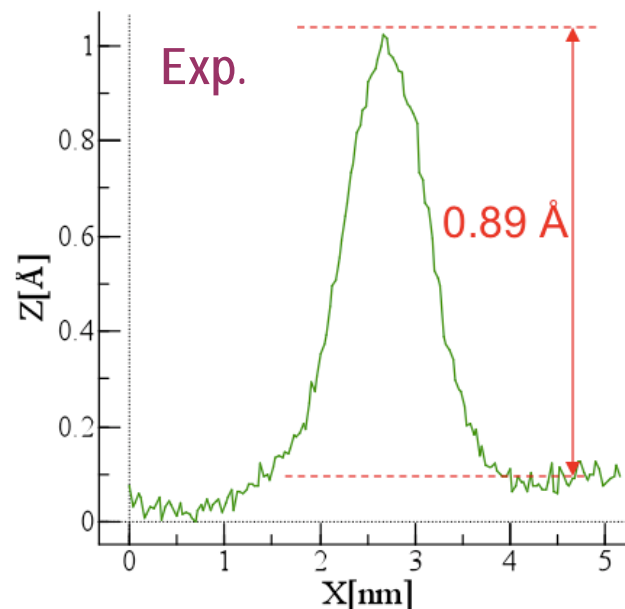
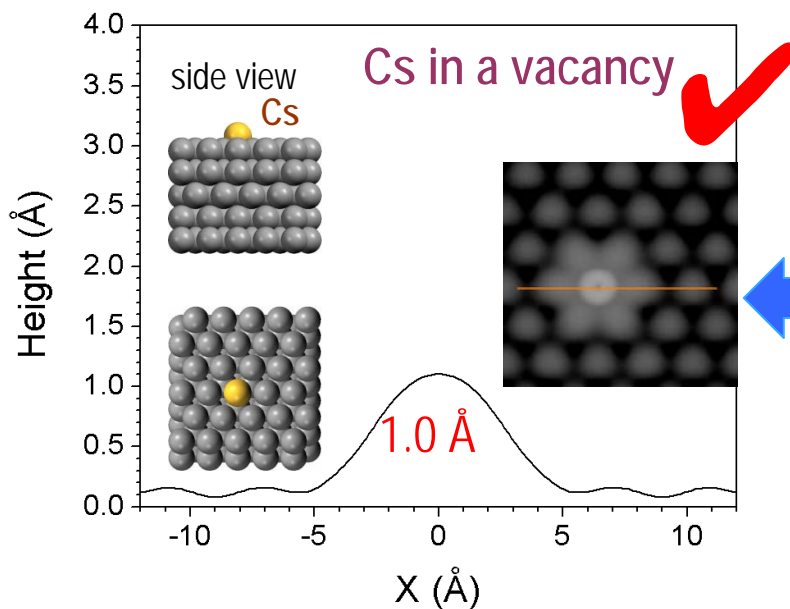
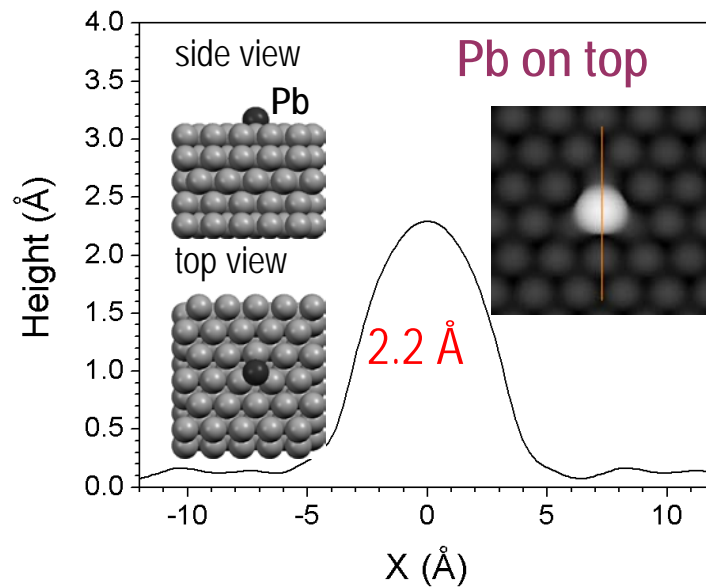
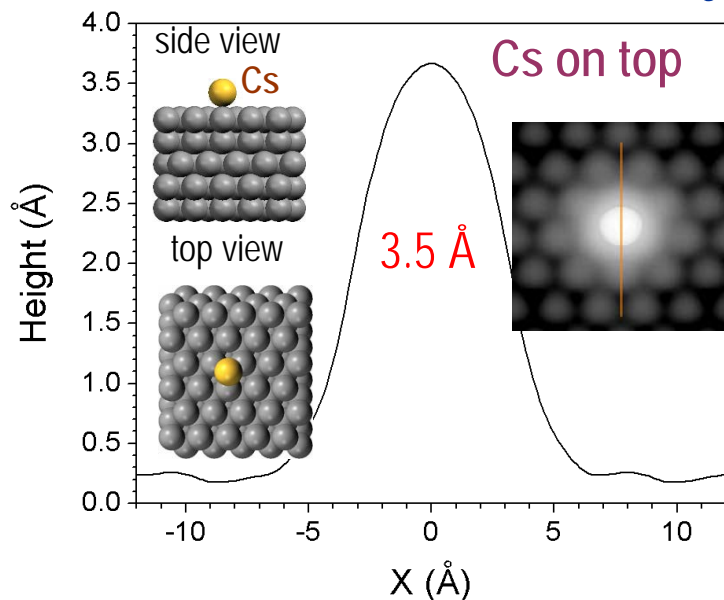


Bare Pb nanomesa on vicinal Si(111)

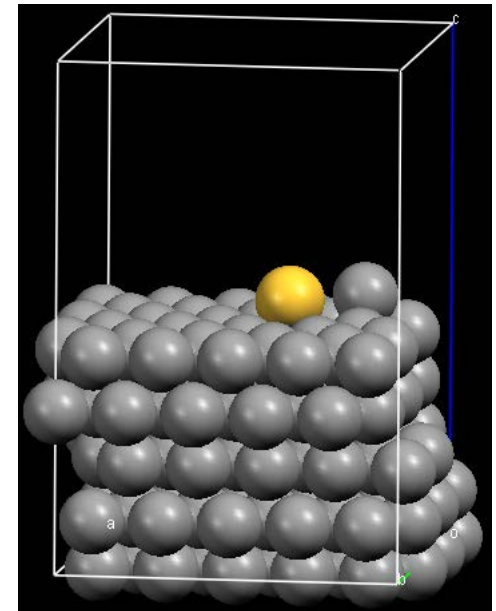
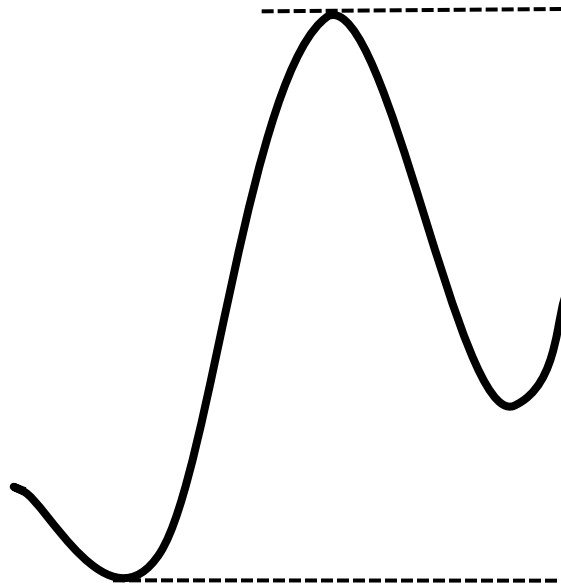
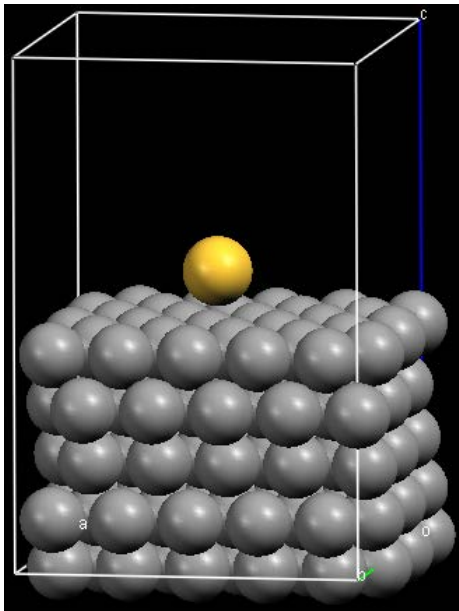


0.057 ML Cs adsorbed

# Identity of the Adatoms



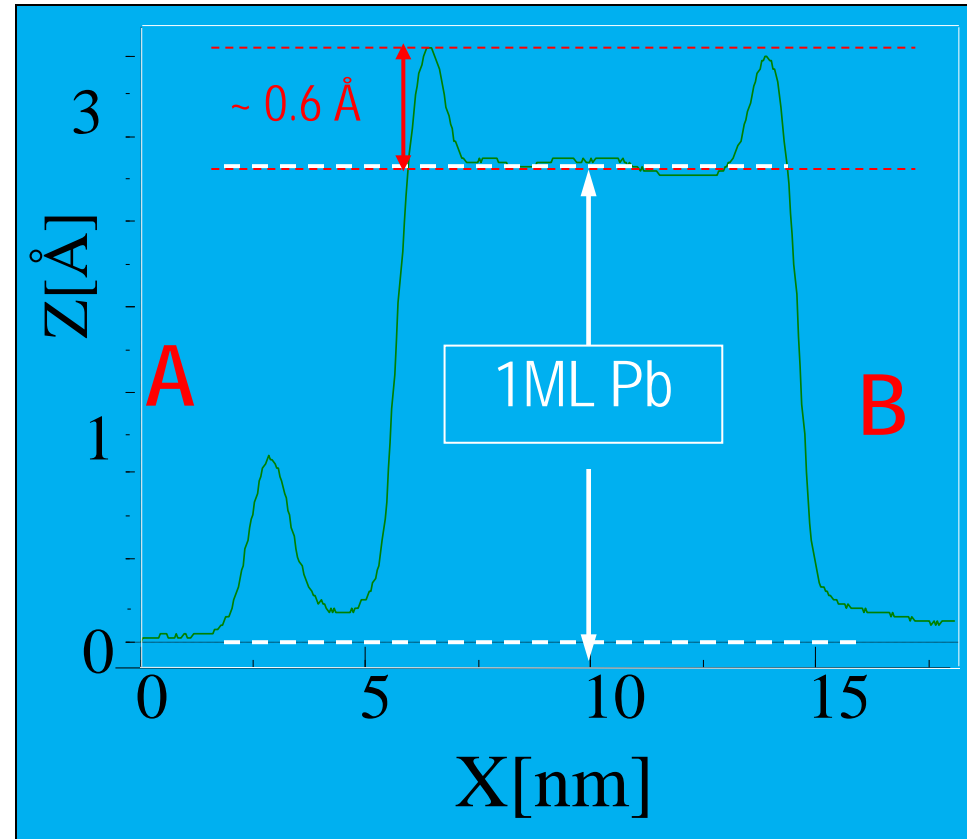
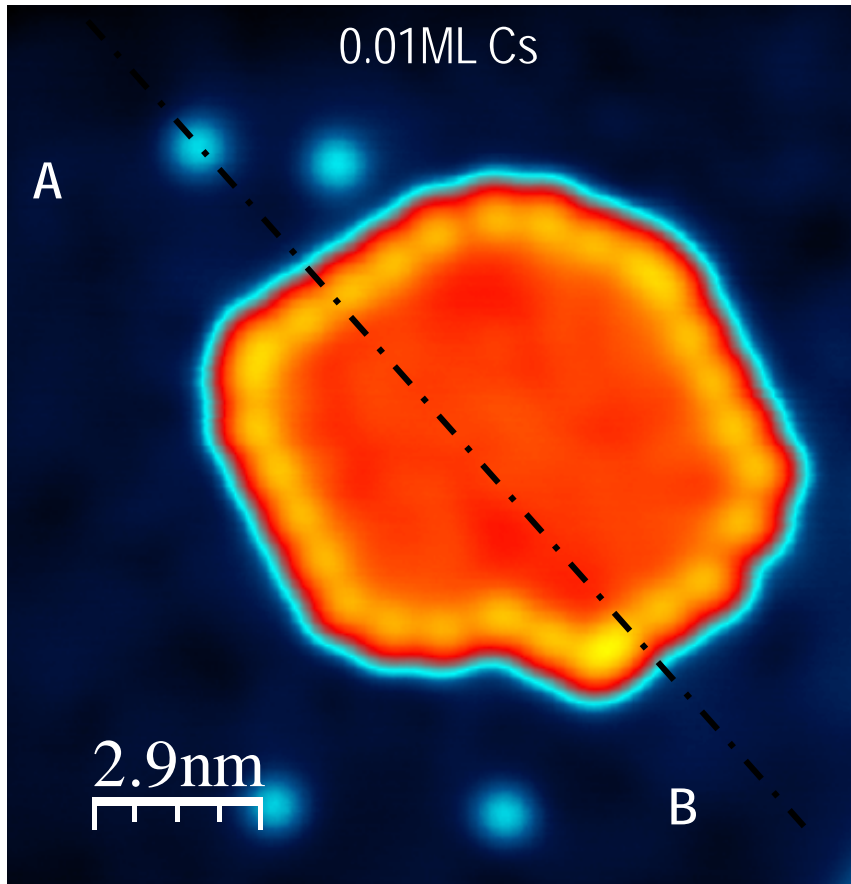
# Fast Enough Kinetics for Surface Alloying



Activation barrier for position exchange: 0.8 eV.



# Elemental Identity of the Emerging Islands



Pb islands with Cs decorated around the steps

# Formation Mechanism of the Emergent Islands

- Cs atoms deposited on the surface of flat-top Pb mesas squeeze out Pb atoms from the top layer (surface alloying), and the expelled Pb atoms nucleate to form the islands (confirmed by counting).
- Due to the relatively lower surface formation energy, the islands prefer to form on the quantum mechanically unstable layers.
- Cs step decoration further reduces the energy cost on the step formation energy of the islands.